



# University of HUDDERSFIELD

## University of Huddersfield Repository

Tran, Van Tung, Yang, Bo-Suk, Oh, Myung-Suck and Tan, Andy

Machine condition prognosis based on regression trees and one-step-ahead prediction

### Original Citation

Tran, Van Tung, Yang, Bo-Suk, Oh, Myung-Suck and Tan, Andy (2007) Machine condition prognosis based on regression trees and one-step-ahead prediction. In: International Symposium on Mechatronics and Automatic Control, 2007, Hochiminh City, Vietnam.

This version is available at <https://eprints.hud.ac.uk/id/eprint/16566/>

The University Repository is a digital collection of the research output of the University, available on Open Access. Copyright and Moral Rights for the items on this site are retained by the individual author and/or other copyright owners. Users may access full items free of charge; copies of full text items generally can be reproduced, displayed or performed and given to third parties in any format or medium for personal research or study, educational or not-for-profit purposes without prior permission or charge, provided:

- The authors, title and full bibliographic details is credited in any copy;
- A hyperlink and/or URL is included for the original metadata page; and
- The content is not changed in any way.

For more information, including our policy and submission procedure, please contact the Repository Team at: [E.mailbox@hud.ac.uk](mailto:E.mailbox@hud.ac.uk).

<http://eprints.hud.ac.uk/>

# MACHINE CONDITION PROGNOSIS BASED ON REGRESSION TREES AND ONE-STEP-AHEAD PREDICTION

Van Tung Tran, Bo-Suk Yang, Myung-Suck Oh  
Andy Chit Chiow Tan \*

School of Mechanical Engineering, Pukyong National University,  
San 100, Yongdang-dong, Namgu, Busan 608-739, South Korea

\* School of Mechanical, Manufacturing and Medical Engineering,  
Queensland University of Technology, G.P.O. Box 2343, Brisbane, Qld. 4001, Australia

## ABSTRACT

Predicting degradation of working conditions of machinery and trending of fault propagation before they reach the alarm or failure threshold is extremely importance in industry to fully utilize the machine production capacity. This paper proposes a method to predict future conditions of machines based on one-step-ahead prediction of time-series forecasting techniques and regression trees. In this study, the embedding dimension is firstly estimated in order to determine the necessary available observations for predicting the next value in the future. This value is subsequently utilized for regression tree predictor. Real trending data of low methane compressor acquired from condition monitoring routine are employed for evaluating the proposed method. The results indicate that the proposed method offers a potential for machine condition prognosis.

*Keywords:* Embedding dimension; Regression trees; Prognosis; Time-series forecasting

## 1. INTRODUCTION

Unexpected catastrophic failures of machine that lead to a costly maintenance or even human casualties can be avoided with the proviso that the machine is appropriately maintained. The most common maintenance strategies are the corrective maintenance and preventive maintenance. However, they are costly and reduce the availability of the machine's productive capability.

Condition-based maintenance involved diagnostic module and prognostic module is an alternative strategy that allows the machine to operate until symptoms of a failure is detected. In this paper, prognosis is the ability to access the current state, forecast the future state, and predict accurately the time-to-failure or the remaining useful life (RUL) of a failing components or subsystems. It is also used to alert warning when the machine condition reaches the predetermined setup alarm or critical

failure threshold. Furthermore, it can be used for running repairs periodically in manufacturing facilities and fault-tolerant control [1]. As result, prognosis has been extensively researched with focus on condition-based maintenance in the recent time.

There are basically two approaches: model-based and data-driven [2-3]. Most of the current approaches concentrate on estimating the RUL and monitoring of signals related to system health. The RUL is the time left for the normal operation of machine before the breakdown occurs or machine condition reaches the critical failure value.

Model-based prognosis techniques required an accurate mathematical model of the failure modes to predict the RUL of critical components. Some of the published researches using those techniques can be found in [4-6] which are merely applied for some specific components and each of them needs a different mathematical model. Furthermore, a suitable

model is also difficult to establish to mimic the real life.

The data-driven approaches are directly derived from routinely monitored system operating data and associated with either statistical or learning techniques. Artificial intelligent techniques are regularly considered due to the flexibility in generating appropriate models in which some of the salient researches have been proposed [7-10].

In order to predict the future state or condition of machine based on available observations, one-step-ahead or multi-step-ahead predictions of time-series forecasting techniques is frequently used. They imply that the estimator utilizes available observations to forecast one value or multiple values at the definite future time. According to Wang [1], the more the steps ahead, the less reliable the forecasting operation is because multi-step prediction is associated with multiple one-step operations. Several methods have been fruitfully proposed for time-series forecasting techniques ranging from statistical to artificial intelligent methods [11-13].

In data-driven approaches, the number of essential observations, so-called embedding dimension  $d$ , is used for forecasting the future value. It should be chosen large enough so that the estimator can forecast accurately the future value and not too large to avoid the unnecessary increase in computational complexity. False nearest neighbor method (FNN) [14] and Cao's method [15] are commonly used to determine the embedding dimension. However, FNN method not only depends on chosen parameters and the number of available observations but also is sensitive to additional noise. Cao's method overcomes the shortcomings of the FNN approach and therefore it is chosen in this study.

Classification and regression tree (CART) [16] is widely implemented in machine fault diagnosis. In the prediction techniques, CART is also applied to forecast the short-term load of the power system [17] with excellent performance. Hence in this paper, CART is proposed as an estimator for machine condition prognosis.

## 2. BACKGROUND KNOWLEDGE

### 2.1. Determine the embedding dimension

Assuming a time-series of  $x_1, x_2, \dots, x_N$ . The time delay vector is defined as follows:

$$y_{i(d)} = [x_i, x_{i+\tau}, x_{i+2\tau}, \dots, x_{i+(d-1)\tau}] \quad (1)$$

$$i = 1, 2, \dots, N - (d-1)\tau$$

where  $\tau$  is the time delay. Defining the quantity as follows:

$$a(i, d) = \frac{\|y_i(d+1) - y_{n(i,d)}(d+1)\|}{\|y_i(d) - y_{n(i,d)}(d)\|} \quad (2)$$

where  $\|\cdot\|$  is the Euclidian distance and is given by the maximum norm,  $y_i(d)$  means the  $i$ th reconstructed vector and  $n(i, d)$  is an integer such that  $y_{n(i,d)}(d)$  is the nearest neighbor of  $y_i(d)$  in the embedding dimension  $d$ . In order to avoid the problems encountered in FNN method, the new quantity is defined as the mean value of all  $a(i, d)$ 's:

$$E(d) = \frac{1}{N - d\tau} \sum_{i=1}^{N-d\tau} a(i, d) \quad (3)$$

$E(d)$  is dependent on only the dimension  $d$  and the time delay  $\tau$ . To investigate its variation from  $d$  to  $d+1$ , the parameter  $E_1$  is given by

$$E_1(d) = \frac{E(d+1)}{E(d)} \quad (4)$$

By increasing the value of  $d$ , the value  $E_1(d)$  is also increased and it stops when the time series comes from a deterministic process. If a plateau is observed for  $d \geq d_0$ ,  $d_0 + 1$  is minimum embedding dimension.

The Cao's method also introduced another quantity  $E_2(d)$  in case that  $E_1(d)$  is slowly increasing or has stopped changing if  $d$  is sufficiently large:

$$E_2(d) = \frac{E^*(d+1)}{E^*(d)} \quad (5)$$

where

$$E^*(d) = \frac{1}{N - d\tau} \sum_{i=1}^{N-d\tau} |x_{i+d\tau} - x_{n(i,d)+d\tau}| \quad (6)$$

### 2.2. Regression trees

In this study, CART is utilized to build up a regression tree model. Beginning with an entire data set, a binary tree is constructed by repeated splits of the subsets into two descendant subsets which are as homogeneous as possible

according to independent variables. Regression tree is built by tree growing and tree pruning.

### 2.2.1. Tree growing

Let  $L$  be a learning sample comprised  $n$  couples of observations  $(y_1, \mathbf{x}_1), \dots, (y_n, \mathbf{x}_n)$ , where  $\mathbf{x}_i = (x_{i_1}, \dots, x_{i_{d_i}})$  is a set of independent variables and  $y_i \in \mathcal{R}$  is a response associated with  $\mathbf{x}_i$ . In order to build the tree, learning sample  $L$  is recursively partitioned by binary split into two subsets until the terminal nodes are achieved. The result is to move the couples  $(y, \mathbf{x})$  to left or right nodes containing more homogeneous responses. The predicted response at each terminal node  $t$  is the mean  $\bar{y}(t)$  of the  $n(t)$  response variables contained in that terminal node. The final structure of a binary tree  $T$  is shown in Fig. 1.

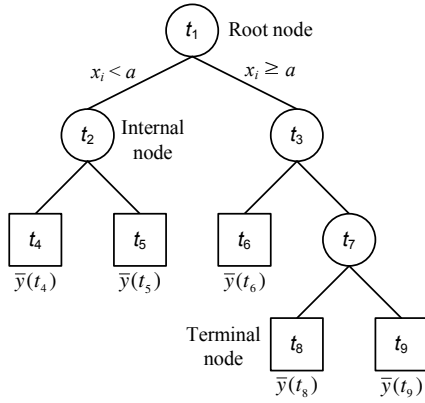


Fig. 1 Binary regression tree  $T$ .

The split selection at any internal node  $t$  is chosen according to the node impurity that is measured by within-node sum of squares:

$$R(t) = \frac{1}{n} \sum_{y_i, \mathbf{x}_i \in t} (y_i - \bar{y}(t))^2 \quad (7)$$

$$\text{and, } \bar{y}(t) = \frac{1}{n(t)} \sum_{y_i, \mathbf{x}_i \in t} y_i \quad (8)$$

When a split is performed, two subsets of observations  $t_L$  and  $t_R$  are obtained. The optimum split  $s^*$  at node  $t$  is obtained from the set of all splitting candidates  $S$  in order that it verifies:

$$\begin{aligned} \Delta R(s^*, t) &= \max_{s \in S} \Delta R(s, t) \\ \Delta R(s, t) &= R(t) - R(t_L) - R(t_R) \end{aligned} \quad (9)$$

where  $R(t_L)$  and  $R(t_R)$  are sum of squares of the left and right subsets, respectively.

### 2.2.2. Tree pruning

The tree gained in tree growing process has many terminal nodes that increase precision of the responses. However, this is frequently too complicated and over-fitting is highly probable. Consequently, it should be pruned back.

Tree pruning process is performed by the following procedure:

*Step 1:* At every internal node, an error-complexity is found for the number of descendant subtrees. The error-complexity is defined as:

$$R_\alpha(T) = R(T) + \alpha |\tilde{T}| \quad (10)$$

where  $R(T) = \frac{1}{n} \sum_{t \in \tilde{T}} \sum_{(y_i, \mathbf{x}_i) \in t} (y_i - \bar{y}(t))^2$  is the total within-node sum of squares,  $\tilde{T}$  is the set of current nodes of  $T$  and  $|\tilde{T}|$  is the number of terminal nodes in  $T$ ,  $\alpha \geq 0$  is the complexity parameter which weights the number of terminal nodes.

*Step 2:* Using the error-complexity attained at step 1, the internal node with the smallest error is replaced by terminal node.

*Step 3:* The algorithm terminates if all the internal nodes have converge to a terminal node. Otherwise, it returns to step 1.

### 2.2.3. Cross-validation for selecting the best tree

There are two possible methods to select the best tree. One is through the use of independent test data and the other is cross-validation that is used in this study.

The learning data  $L$  is randomly divided into  $v$  approximately equal group, and  $(v-1)$  groups are then utilized as the learning data for growing the tree model. The remaining group is employed as testing data for error estimation of tree model. As a result,  $v$  errors are obtained by  $v$  iterations with variation of the combinations of the learning data and testing data. The mean and standard deviation of the errors are given:

$$R^{CV}(d) = \frac{1}{v} \sum_{i=1}^v R^{ts}(d_i) \quad (11)$$

$$\sigma(R^{CV}(d)) = \sqrt{\frac{1}{v} \sum_{i=1}^v (R^{ts}(d_i) - R^{CV}(d))^2}$$

Here  $R^{CV}(\cdot)$  is the average relative error,  $d$  is the cross-validation tree,  $\sigma$  is the standard error, and  $R^{ts}(\cdot)$  is the testing data error. The best tree  $T_t$  selection is adopted:

$$R(T_t) = R^{CV}(T_{\min}) + \sigma(R^{CV}(T_{\min})) \quad (12)$$

where  $R(\cdot)$  is the cross-validation error,  $T_{\min}$  is the tree with the smallest cross-validation error.

### 3. PROPOSED SYSTEM

Normally when a fault occurs, the conditions of machine can be identified by the change in vibration amplitude. In order to predict the future state based on available vibration data, the proposed system as shown in Fig. 2 which consists of four procedures is proposed.

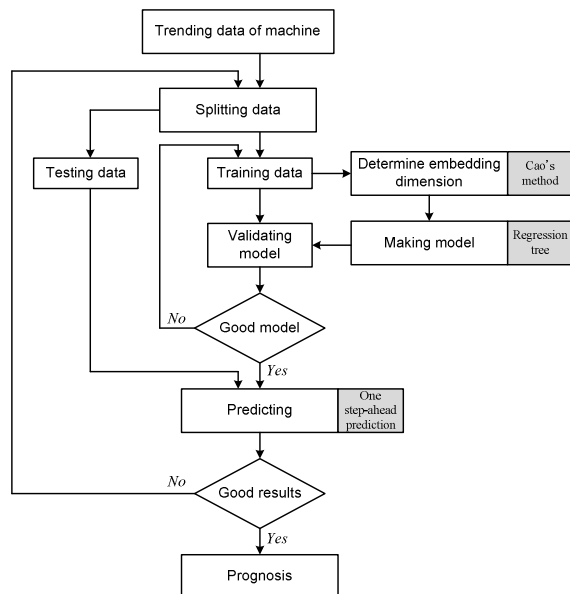


Fig. 2 Proposed system for machine fault prognosis.

The role of each procedure is explained as follows:

*Step 1 Data acquisition:* acquiring vibration signal during the running process of the machine until faults occur.

*Step 2 Data splitting:* the trending data is split into two parts: training data for building the

model and testing data for testing the validated model.

*Step 3 Training-validating:* determining the embedding dimension based on Cao's method, building the model and validating the model for measuring the performance capability.

*Step 4 Predicting:* one-step-ahead prediction is used to forecast the future value. The predicted result is measured by the error between predicted value and actual value in the testing data. If the prediction is successful, the result obtained from this procedure is the prognosis system.

### 4. EXPERIMENTS AND RESULTS

The proposed method is applied to real system to predict the trending data of a low methane compressor. This compressor shown in Fig. 3 and its specification is summarized in Table 1.

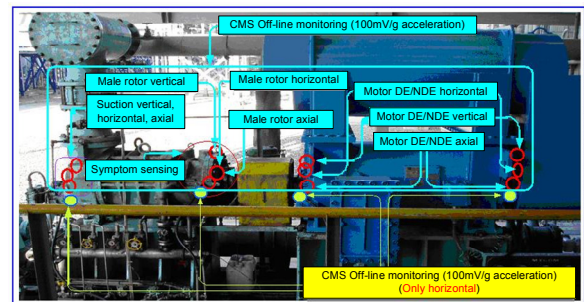


Fig. 3 Low methane compressor.

The data applied in this study is peak acceleration and envelope acceleration trending data recorded from August 2005 to November 2005 as shown in Figs. 4 and 5. Consequently, it can be seen as time-series data.

Table 1 Description of system

Electric motor		Compressor	
Voltage	6600 V	Type	Wet screw
Power	440 kW	Lobe	Male rotor (4 lobes)
Pole	2 Pole		Female rotor (6 lobes)
Bearing	NDE:#6216, DE:#6216	Bearing	Thrust: 7321 BDB
RPM	3565 rpm		Radial: Sleeve type

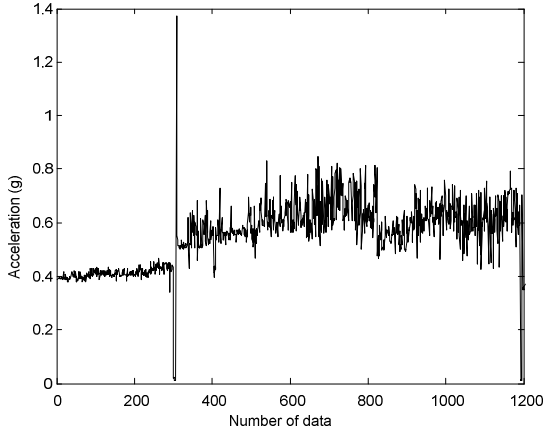


Fig. 4 The entire of peak acceleration data of low methane compressor.

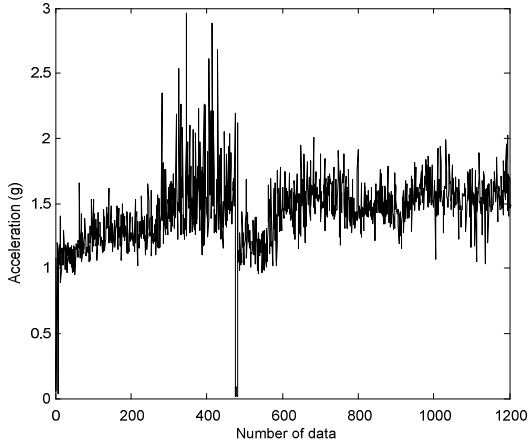


Fig. 5 The entire of envelope acceleration data of low methane compressor.

The machine is in normal condition during the first 300 points. After that time, the condition of machine suddenly changes indicating some faults occurring in this machine. With the aim of forecasting the change of machine condition, the first 300 points were used to train the system and the following 150 points were employed for testing system.

The predicting performance is evaluated by using the root-mean square error (RMSE) given as:

$$RMSE = \sqrt{\frac{\sum_{i=1}^N (y_i - \hat{y}_i)^2}{N}} \quad (13)$$

where  $N$  represents the total number of data points,  $y_i$  is the response value in observations and  $\hat{y}_i$  represents the predicted value of the model.

The time delay value is chosen as 1 for the reason that one step-ahead is implemented in all

datasets. Furthermore, the number of cases for each terminal node in tree growing process is 5 and 10 cross-validations are decided for selecting the best tree in tree pruning.

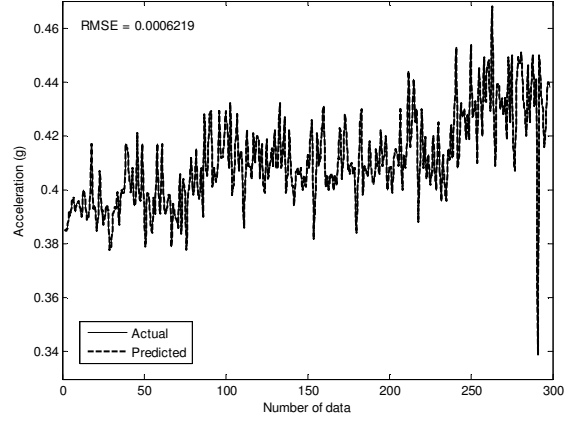


Fig. 6 Training and validating results of peak acceleration data (the first 300 points).

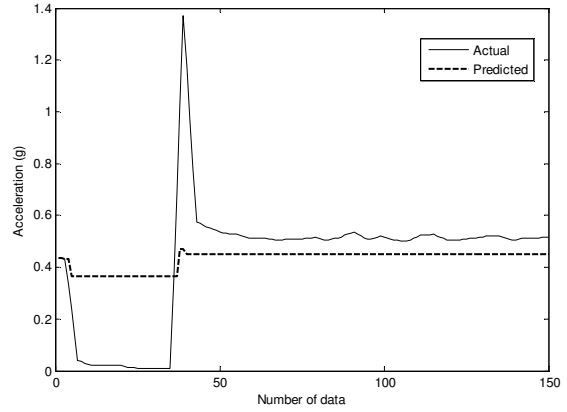


Fig. 7. Predicted results of peak acceleration data.

Excellent validating performance is shown in Fig. 6 with a small RMSE value of 0.00062. However, in the testing process, an unexpected result occurs as depicted in Fig. 7. It shows that the model is incapable of predicting the future value. The reason is that the model could be improperly trained because the training data does not contain anomalous values. This affirmation could be demonstrated by using another data set consisting of those anomalous values. The embedding dimension is estimated to be 6 when the values of  $E_1(d)$  reaches its saturation as depicted in Fig. 8. Figs. 9 and 10 are the validating and testing model, respectively. The training and validating results of peak acceleration data are almost identical, as shown in Fig. 9, with a very small RMSE value

of 0.000601. In the testing process, even though the model cannot predict accurately the machine condition, the RMSE value is 0.0143 which is acceptable as revealed in Fig. 10.

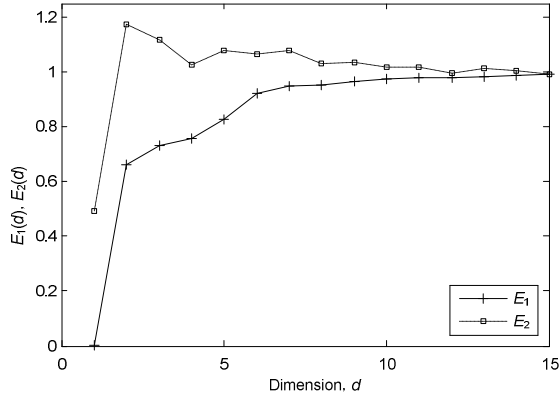


Fig. 8 The values of  $E_1$  and  $E_2$  of peak acceleration data of low methane compressor.

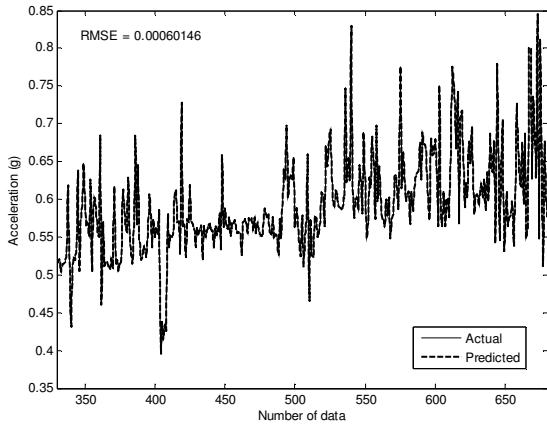


Fig. 9 Training and validating results of peak acceleration data.

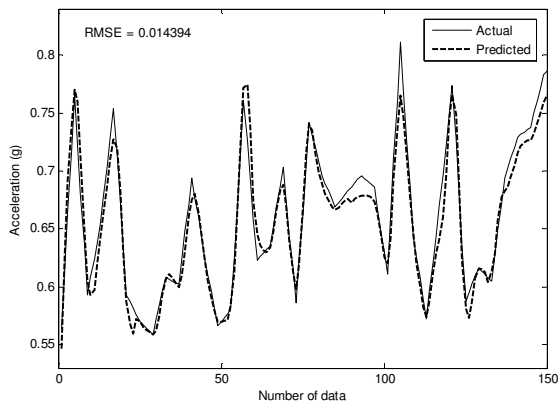


Fig. 10 Predicted results of peak acceleration data.

By using the similar processes with the embedding as 6, validating model and testing

model are respectively carried out and the final results are obtained in Figs. 11 and 12. These results closely resembled the actual data with a RMSE error of 0.000291, as shown in Fig. 11. Although the predictor is incapable of predicting the machine condition precisely, it can closely track the changes of trending condition of machine with a small error of 0.06 as shown in Fig. 12.

Fig. 12 Data trending of envelope acceleration of low methane compressor.

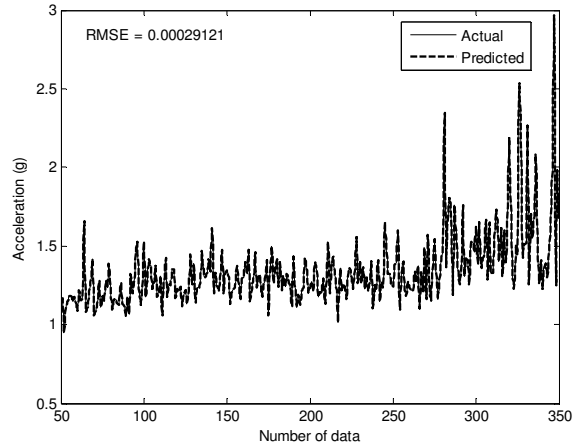


Fig. 11 Training and validating results of envelope acceleration data.

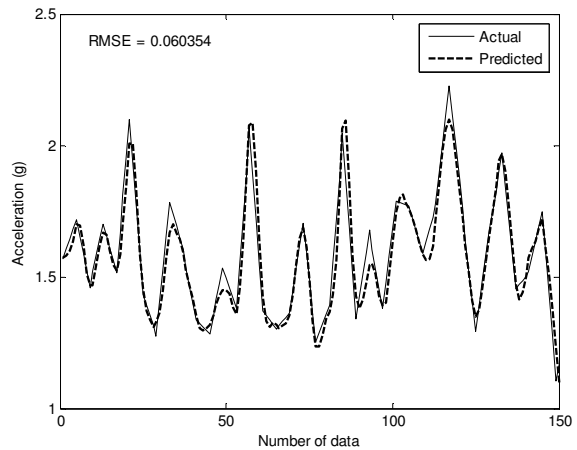


Fig. 12 Predicted results of envelope acceleration data.

## 5. CONCLUSIONS

Machine condition prognosis is extremely significant in foretelling the degradation working condition and trends of fault propagation before they reach the alarm. In this study, the machine prognosis based on one-step-

ahead of time-series techniques and regression trees has been investigated. The proposed method is validated by predicting future state condition of a low methane compressor wherein the peak acceleration and envelope acceleration have been examined. Using an embedded dimension of 6, the results give a prediction error of 1.43% with peak acceleration data, and 6% with the enveloped acceleration data. These errors are small in statistical sense. The results confirm that the proposed method offers a potential for machine condition prognosis with one-step-ahead prediction.

### ACKNOWLEDGEMENT

This work was partially supported by the NURI project in 2007

### REFERENCES

1. W. Wang, An adaptive predictor for dynamic system forecasting, *Mechanical Systems and Signal Processing* 21 (2007) 809–823.
2. G. Vachtsevanos, F. Lewis, M. Roemer, A. Hess, B. Wu, *Intelligent fault diagnosis and prognosis for engineering system*, Wiley, 2006.
3. J. Luo, M. Namburu, K. Pattipati, Liu Qiao, M. Kawamoto, S. Chigusa, Model-based prognostic techniques, *AUTOTESTCON Proceedings, IEEE Systems Readiness Technology Conference*, 22-25 Sept. (2003) 330–340.
4. M. Watson, C. Byington, D. Edwards, S. Amin, Dynamic modeling and wear-based remaining useful life prediction of high power clutch systems, *Tribology Transactions* 48 (2005) 208–217.
5. M. Luo, D. Wang, M. Pham, C.B. Low, J.B. Zhang, D.H. Zhang, Y.Z. Zhao, Model-based fault diagnosis/prognosis for wheeled mobile robots: a review, *Industrial Electronics Society ,32<sup>nd</sup> Annual conference of IEEE*, 6-10 Nov. (2005) 2267–2272.
6. Y. Li, T.R. Kurfess, S.Y. Liang, Stochastic prognostics for rolling element bearings, *Mechanical Systems and Signal Processing* 14 (2000) 747–762.
7. G. Vachtsevanos, P. Wang, Fault prognosis using dynamic wavelet neural networks, *AUTOTESTCON Proceedings, IEEE Systems Readiness Technology Conference*, 22-23 Aug. (2001) 857–870.
8. R. Huang, L. Xi, X. Li, C. R. Liu, H. Qiu, J. Lee, Residual life prediction for ball bearings based on self-organizing map and back propagation neural network methods, *Mechanical Systems and Signal Processing* 21 (2007) 193–207.
9. W.Q. Wang, M.F. Golnaraghi, F. Ismail, Prognosis of machine health condition using neuro-fuzzy system, *Mechanical System and Signal Processing* 18 (2004) 813–831.
10. B. Satish, N.D.R. Sarma, A fuzzy BP approach for diagnosis and prognosis of bearing faults in induction motors, *IEEE Power Engineering Society General Meeting 3* (2005) 2291–2294.
11. U. Thissen, R. van Brakel, A.P. de Weijer, W.J. Melssen, L.M.C. Buydens, Using support vector machines for time series predicting, *Chemometrics and Intelligent Laboratory Systems* 69 (2003) 35–49.
12. Dulakshi S.K. Karunasinghea, Shie-Yui Liongb, Chaotic time series prediction with a global model: Artificial neural network, *Journal of Hydrology* 323 (2006) 92–105.
13. G. Simon, J.A. Lee, M. Cottrell, M. Verleysen, Forecasting the CATS benchmark with the Double Vector Quantization, *Neurocomputing*, in press.
14. M.B. Kennel, R. Brown, H.D.I. Abarbanel, Determining embedding dimension for phase-space reconstruction using a geometrical construction, *Physical Review A* 45 (1992) 3403–3411.
15. L. Cao, Practical method for determining the minimum embedding dimension of a scalar time series, *Physica D* 110 (1997) 43–50.
16. L. Breiman, J.H. Friedman, R.A. Olshen, C.J. Stone, *Classification and regression trees*, Chapman & Hall (1984).
17. J. Yang, J. Stenzel, Short-term load forecasting with increment regression tree, *Electric Power Systems Research* 76 (2006) 880–888.