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1 Ablation of submicrometer holes using an extreme-ultraviolet laser

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10 Simulations and experiments are used to study extreme ultraviolet laser drilling of
11 sub-micrometer holes. The ablation process has been studied with a 2D Eulerian
12 hydrodynamic code that includes bound-free absorption processes relevant to the
13 interaction of EUV lasers with a solid material. Good agreement is observed between
14 the simulated and measured ablated depths for on target irradiances of up to $1 \times$
15 10^{10} W cm⁻². An increase in the irradiance to 1×10^{12} W cm⁻² is predicted to
16 ablate material to a depth of 3.8 μ m from a single pulse with a hole diameter 3
17 to 4 times larger than the focal spot size. The model allows for the simulation of
18 the interaction of a laser pulse with the crater created by a previous shot. Multiple
19 pulse, lower fluence irradiation configurations under optimized focusing conditions,
20 i.e. approaching the diffraction limit, are shown to be advantageous for applications
21 requiring mesoscale (100nm-1 μ m) features and a high level of control over the ablation
22 profile.

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24 I. INTRODUCTION

25 Considerable advances have been made in high fluence extreme ultra-violet (EUV) and
26 X-ray laser technology as is shown by laser plasma based EUV lasers¹, free-electron lasers²
27 and capillary discharge lasers³⁻⁶. With higher fluences and repetition rates up to 100Hz⁷
28 now available, EUV and X-ray lasers can be used to directly generate strongly coupled
29 plasmas. Targets irradiated by EUV lasers are heated predominantly via direct photo-
30 ionization, as opposed to inverse bremsstrahlung as with traditional optical, infra-red (IR)
31 and ultraviolet (UV) lasers. This results in typically lower plasma temperatures and higher
32 particle densities⁸. With traditional laser produced plasmas, an expanding plume of plasma
33 only allows absorption away from the target surface where the electron density has dropped
34 below a critical value ($\simeq 10^{21}/\lambda_\mu^2 \text{ cm}^{-3}$, where λ_μ is the laser wavelength in units of microns).
35 By reducing the wavelength into the EUV/X-ray region, the critical electron density is
36 typically greater than solid and the laser photon energy, E_p , becomes sufficient to directly
37 photo-ionise elemental components (ionisation energy E_i), transferring energy ($E_p - E_i$) to
38 the ejected electron. As the critical electron density (the point at which the real part of the
39 dielectric function goes to zero) is typically higher than solid, the laser is able to penetrate
40 the expanding plasma plume and continue to heat the solid material directly throughout the
41 duration of the laser pulse. This differs from the interaction of optical, IR and UV pulses
42 with solids where the majority of the pulse energy is absorbed within the expanding plasma
43 plume via inverse bremsstrahlung. Reducing the lasing wavelength to the EUV/soft X-ray
44 region also allows for a tighter focus, due to a reduction in the diffraction limit. The tighter
45 focus is a potentially desirable property for a number of applications, for example, mesoscale
46 machining⁹, mass spectrometry¹⁰ and the coating of refractory material onto substrates.

47 In order to promote research and to accelerate the development of industrial applications,
48 there is a significant motivation to produce compact and affordable EUV/X-ray laser sources
49 for use in parallel with large scale free electron laser facilities such as the European free
50 electron laser, FLASH¹¹. One such example is a table-top size soft X-ray laser system^{12,13}
51 based upon capillary discharge excitation of an Ar gas which causes lasing at 46.9nm with
52 a pulse energy up to 0.8mJ^{3,6} and a pulse length of 1.2ns⁴.

53 The work presented here utilises a novel combination of fluid code modelling with atomic
54 physics to simulate EUV/soft X-ray interaction with a solid, the laser energy deposition

55 within the target, thermal energy transport and the subsequent ablative flow away from
56 the target. Using a 2D hydrodynamic code, POLLUX¹⁴⁻¹⁶, originally written to simulate
57 optical and infra-red laser interaction, and adding new absorption and atomic physics enables
58 the simulation of the ablative properties of EUV and X-ray lasers. A comparison between
59 simulation and experiment is shown for a capillary discharge laser, operating at 46.9nm,
60 ablating a planar parylene-N target under vacuum. Simulation results are then presented
61 for higher irradiance and multiple pulse interactions demonstrating the significant potential
62 benefits of capillary discharge lasers for high aspect ratio hole drilling.

63 II. POLLUX

64 The 2D Eulerian hydrodynamic code POLLUX, originally written at the University of
65 York, was developed to model moderate irradiance ($10^9 - 10^{14} \text{ W cm}^{-2}$) optical and infra-red
66 laser irradiation of a solid target. With optical lasers, a strongly ionized plasma is produced
67 which absorbs the incident laser beam. The code solves the three first-order quasi-linear
68 partial differential equations of hydrodynamic flow using the flux corrected transport model
69 of Boris and Book¹⁷ with an upwind algorithm¹⁸ for the first term. Energy absorption within
70 the target has been modified to include photoionization processes relevant to EUV and X-ray
71 interactions. Energy is absorbed by the plasma electrons through inverse bremsstrahlung
72 and direct photo-ionization and distributed via electron-ion collisions. The energy transfer
73 rate between electrons and ions is calculated using the smaller value of the Spitzer electron
74 collision frequency¹⁹ or the electron-phonon collision frequency²⁰. For calculation of the
75 equation-of-state (EOS) variables, POLLUX utilizes in-line hydrodynamic EOS subroutines
76 from the Chart-D²¹ equation-of-state package developed at Sandia National Laboratories and
77 includes two phase transitions.

78 To properly calculate bound-free absorption processes within the target material, a model
79 of atomic structure is used to account for transitions from both the ground and excited states.
80 To achieve this, whilst keeping the runtime reasonable for a fluid code, a superconfiguration
81 model²² has been employed to reduce the number of levels to be considered. Ionisation de-
82 pendant superconfigurations are calculated for an individual element by using the Flexible
83 Atomic Code (FAC)²³ to solve the radial wavefunction. This provides detailed atomic struc-
84 ture, which is then post-processed to form a reduced data set of ionisation stages, atomic

85 energy levels and photoionization cross-sections. As the produced plasma is close to solid
86 density, the ionization energy, E_i , can be significantly lowered due to the presence of the
87 surrounding electrons and ions. This ionization potential depression can cause pressure ion-
88 ization, thus reducing the absorption of the laser in that region. Ion potential depression
89 is accounted for using a modified model originally developed by Stewart and Pyatt²⁴. Ionic
90 and excited state populations are determined by assuming local thermodynamic equilibrium
91 (LTE) and using the Saha-Boltzmann relation. Although the initial plasma state is highly
92 non-equilibrated, it has been shown that due to the high densities involved, the plasma
93 ionization equilibrates on a time-scale of tens of femtoseconds²⁵. The fluid code simulations
94 shown here operate on a hydrodynamic time-scale of > 1 ps, therefore the LTE assumption
95 is valid. An analytical approximation of the Kramers-Kronig relationship is used to deter-
96 mine temperature dependant atomic scattering factors and thus the refractive index of the
97 plasma, and has been reported previously²⁶. This combination of atomic physics modelling
98 of laser absorption, EUV ray-tracing within the plasma including a temperature dependant
99 refractive index and the simulation of the subsequent ablative flow from the target is a
100 unique capability for the application of mesoscale machining.

101 III. EXPERIMENTAL BENCHMARKING

102 The benchmark simulation results shown here are for an Ar-based capillary discharge laser
103 irradiating a planar parylene-N target, with a photon energy of 26.4 eV ($\lambda = 46.9$ nm), a
104 FWHM pulse length of 1200ps, and fluence ranging between 2 and 8 J cm⁻². Experimental
105 measurements of the ablated depth in Parylene-N were conducted using a capillary discharge
106 laser system developed at Colorado State University (CSU)⁵.

107 The capillary discharge laser was focused, under vacuum, using a Fresnel zone plate with
108 a numerical aperture of 0.12, where the smallest possible diameter of the first null of the
109 Airy disk is ~ 240 nm. The spatial profile of the laser in the simulations is described by
110 approximating the central lobe of the Airy disk as a Gaussian function. The diffraction
111 limited spot size in this case would be a FWHM diameter of ~ 207 nm. In the experiments,
112 craters with a FWHM diameter ranging between 650 and 850nm were ablated.

113 By varying the fluence over the range tested via experimental measurement, a comparison
114 can be made to ascertain the accuracy of the code in the simulation of EUV ablation. Figure

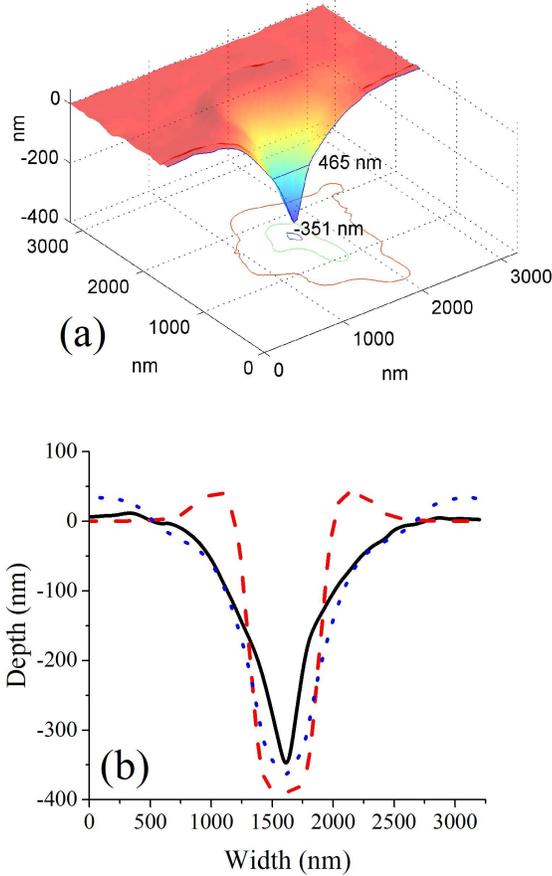


Figure 1. (Color online) (a) Experimentally obtained ablation profile. The FWHM and depth of the hole are indicated. The contours are cross sections of the ablated crater at 10, 50 and 90 percent of its depth. (b) Comparison with the simulated ablation profile, for a fluence of 7.7 J cm^{-2} ($6 \times 10^9 \text{ W cm}^{-2}$). The black solid line in (b) is a lineout of the experimental profile in (a). Simulated ablation profiles are shown for a laser with a Gaussian beam profile (red dashed) and a double Gaussian approximation of the central lobe (containing 92% of total energy) and side lobe (containing 8% of the total energy) of an Airy disk (blue dotted).

115 1(a) shows an image of an ablated parylene-N target measured using atomic force microscopy
 116 (AFM), after the shot, for the fluence of 7.7 J cm^{-2} . The corresponding line-out through the
 117 central ablated region is shown (figure 1(b)) with a comparison to two computed ablation
 118 profiles. The first using a Gaussian profile as described and the second using a double
 119 Gaussian profile to approximate an Airy pattern with 92% of the energy in the central lobe
 120 and 8% of the energy in a side lobe. Figure 2 shows a comparison between the ablated depth
 121 in Parylene-N measured experimentally and the ablated depth predicted through simulation.

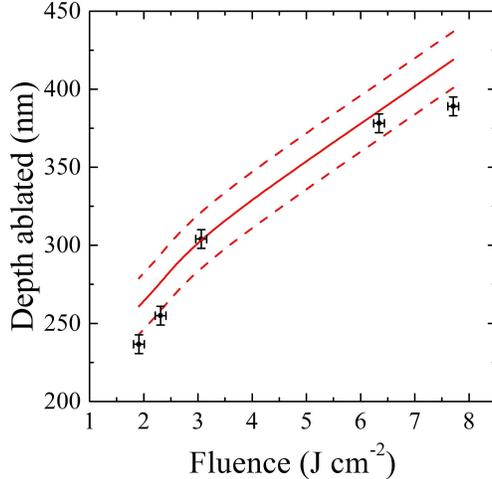


Figure 2. (Color online) Comparison between experimental ablated depth measurements (squares) and simulations (solid line) as a function of EUV laser fluence on target. The dashed lines indicate the resolution of the Eulerian mesh used in the simulations.

122 The depth of ablation in the simulation is taken after 1300ps ($t = 600$ ps is the peak of the
 123 pulse) at the point at which the ion temperature drops below the melting point, which for
 124 Parylene-N is 0.06eV ($420^{\circ}C$). The dashed lines indicate the resolution of the Eulerian mesh
 125 used in the simulations which is limited by the Courant-Friedrichs-Lewy condition²⁷.

126 Good agreement is observed between the ablated depth predicted via simulation and the
 127 experimentally observed ablated depth, giving confidence to the computational algorithms
 128 utilised. Current capillary discharge lasers are capable of pulse energies up to 0.8 mJ⁶, hence
 129 irradiances approaching 1×10^{12} W cm⁻² could be achievable with appropriate collection
 130 and focussing optics.

131 IV. SIMULATION RESULTS AND DISCUSSION

132 To explore the ablative capabilities of this technology, the effect of varying the irradiance
 133 from 1×10^9 W cm⁻² to 1×10^{12} W cm⁻² has been simulated, the results of which
 134 are shown in figure 3. Ablated depths of $3.8 \mu\text{m}$ per pulse are observed for the highest
 135 irradiance with a lateral hole size of $2.2 \mu\text{m}$ (FWHM) for a $0.5 \mu\text{m}$ diameter (FWHM) focal
 136 width. High aspect ratio, sub-micron size surface features are achievable, providing the
 137 system is optimised to inhibit lateral heat transport within the target. Figure 3 shows
 138 ablation profiles as a function of irradiance after 1300 ps of irradiation and demonstrates

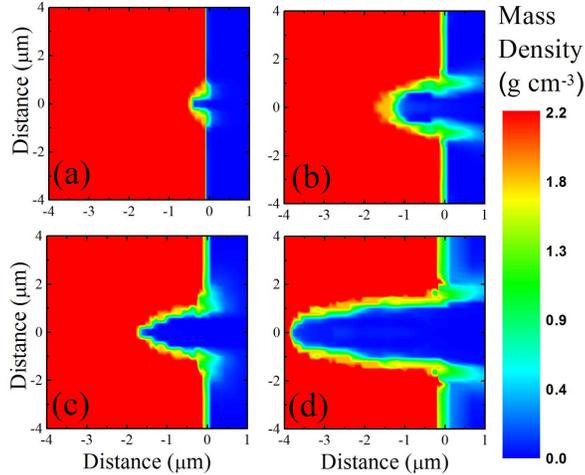


Figure 3. (Color online) Simulated ablation profiles at $t = 1300\text{ps}$ for (a) $1 \times 10^9 \text{ W cm}^{-2}$, (b) $1 \times 10^{10} \text{ W cm}^{-2}$, (c) $1 \times 10^{11} \text{ W cm}^{-2}$ and (d) $1 \times 10^{12} \text{ W cm}^{-2}$ with a focal spot diameter of 500nm.

139 that lateral heat transport increases the feature size with increasing fluence as one would
 140 expect due to the increase in localised energy deposition in the target. Typical predicted
 141 temperatures for the laser produced plasma range between 2 and 20eV with plasma flow
 142 velocities along the laser axis ranging between 10^5 to 10^7 cm s^{-1} , depending upon the laser
 143 irradiance. Further information regarding the plasma properties can be found in previously
 144 published work^{16,26}.

145 Ablation with a laser operating in the EUV wavelength range optimises energy deposition
 146 within the target. Parylene-N has $> 70\%$ transparency over the range of optical wavelengths,
 147 whereby photons at 46.9nm have a penetration depth of only 20nm in cold solid parylene-N.
 148 This leads to a highly localised deposition of energy in small volume, resulting in increased
 149 uniformity of heating and thus ablation. As the target material is heated, via bound-free
 150 absorption dominated by the carbon component of the material, ionization increases and the
 151 material becomes transparent as the 26.4eV photon energy is only sufficient to ionise carbon
 152 to a C^{2+} state. This 'bleaching' effect allows the EUV laser to ablate a significant amount
 153 of material in a single pulse, resulting in high aspect ratio drilling. Plasma refractive index
 154 effects are found to be negligible for 26.4eV photons in parylene-N for irradiances below
 155 $10^{10} \text{ W cm}^{-2}$. Above this irradiance, focussing and de-focussing effects occur in different
 156 regions of the plasma which in part contributes to the enlarging of the surface feature size.
 157 The additional heating due to the higher irradiance results in the dominant ionization stage

158 in the plasma being C^{4+} or higher and thus the free electron density becomes comparable
159 to the critical density of the EUV laser and further reduces the efficacy of the laser energy
160 deposition. At lower irradiance, the dominant ionisation stage is lower, the free electron
161 density remains sub-critical and the real component of the dielectric function remains greater
162 than zero.

163 Over 85% of the ablation is seen to occur within the first half of the laser pulse for
164 the parameters shown in figure 4, and as lateral heat transport dominates at later times,
165 shortening the pulse length would inhibit the enlarging of the feature size by reducing the
166 damaging thermal effects. Alternatively, multiple low fluence pulses could be used to inhibit
167 lateral heat transport, reducing the surface feature size and enabling high aspect ratio, sub-
168 micron sized ablation. To enable multi-pulse simulation, a post-processor has been developed
169 to configure the output of a single pulse simulation. The post-processor analyses output after
170 the end of the first laser pulse, 'removing' any plasma with a temperature greater than the
171 melting point of parylene-N, i.e. resetting the temperature to room (0.025eV) and the
172 density to that of the vacuum ($10^{-7} \times \rho_{solid}$). The simulation is then restarted for a second
173 pulse interacting with the existing ablation crater. Figure 5 indicates how a multiple pulse
174 technique can be utilised to ablate with high uniformity (approximately constant width over
175 ablated depth) and improved surface feature size. Figures 5(a) and 5(b) show the ablation
176 profiles after 1 and 4 pulses respectively, with a focal spot diameter (FWHM) of 500nm and
177 an irradiance of $5 \times 10^9 \text{ W cm}^{-2}$. After 4 pulses, a depth of $4.2 \mu\text{m}$ has been ablated with a
178 lateral hole size of $1.3 \mu\text{m}$ (FWHM). This hole size will reduce further as the diffraction limit
179 is approached, as shown in figures 5(c) and 5(d). Figures 5(c) and 5(d) show the ablation
180 profiles for a beam of the same irradiance with a focal spot diameter of 200nm after 1 and 2
181 pulses respectively. An ablated depth of $2.4 \mu\text{m}$ is observed after 2 pulses, with a lateral hole
182 size of 644nm (FWHM). This indicates the potential of this technology for sub-micron size
183 hole drilling under optimised focussing conditions. Using the computational environment
184 described above, the ablative characteristics can be readily optimised depending upon the
185 requirements of the application.

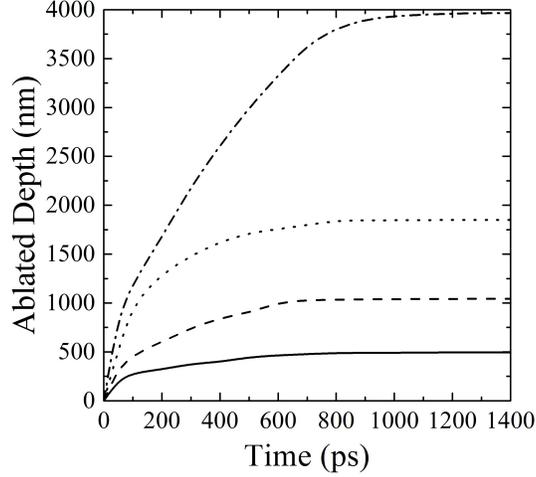


Figure 4. Simulated ablated depth per pulse as a function of time and irradiance for $1 \times 10^9 \text{ W cm}^{-2}$ (solid), $1 \times 10^{10} \text{ W cm}^{-2}$ (dashed), $1 \times 10^{11} \text{ W cm}^{-2}$ (dotted) and $1 \times 10^{12} \text{ W cm}^{-2}$ (dash-dot). The pulse length is 1200ps and the focal spot diameter is 500nm.

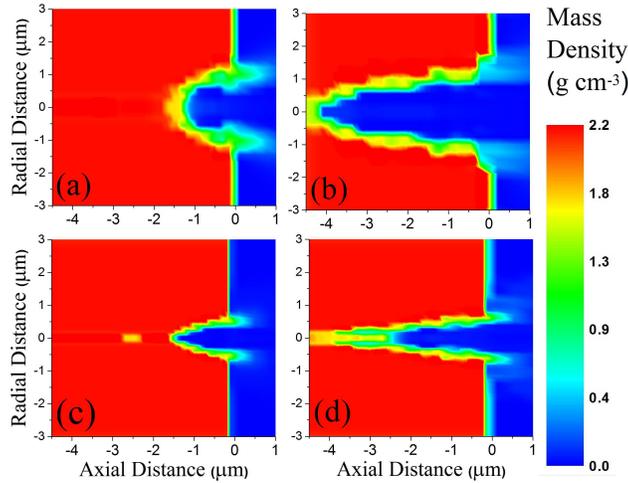


Figure 5. (Color online) Simulated ablation profiles at $t = 1300\text{ps}$ with an irradiance of $5 \times 10^9 \text{ W cm}^{-2}$ for focal spot diameters of 500nm after (a) 1 pulse and (b) 4 pulses, and 200nm after (c) 1 pulse and (d) 2 pulses.

186 **V. CONCLUSION**

187 This work has demonstrated how a fluid code combined with relevant atomic physics has
 188 been used to simulate the heating and subsequent ablation induced by a capillary discharge
 189 laser with a photon energy of 26.4 eV. Good agreement is observed between the ablated

190 depth measured experimentally and the predicted depth obtained via simulation for on
191 target irradiances of up to $6 \times 10^9 \text{ W cm}^{-2}$. Increasing the irradiance in the simulation to 1
192 $\times 10^{12} \text{ W cm}^{-2}$ has shown an increase in surface feature size due to lateral heat transport.
193 Over 85% of the ablation occurs within the first half of the 1200ps laser pulse and lateral heat
194 transport increases at later time increasing the surface feature size further. Multiple, lower
195 fluence pulses under optimised focussing conditions will be advantageous for applications
196 requiring high-aspect ratio, mesoscale (100nm - $1\mu\text{m}$) features and a high level of control
197 over the ablation profile.

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