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Costs and efficiency in English higher education: An analysis using latent class stochastic frontier models

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# COSTS AND EFFICIENCY IN ENGLISH HIGHER EDUCATION

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Inspiring tomorrow's professionals

## AN ANALYSIS USING LATENT CLASS STOCHASTIC FRONTIER MODELS

*INFORMS Annual Meeting,*

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Inspiring tomorrow's professionals



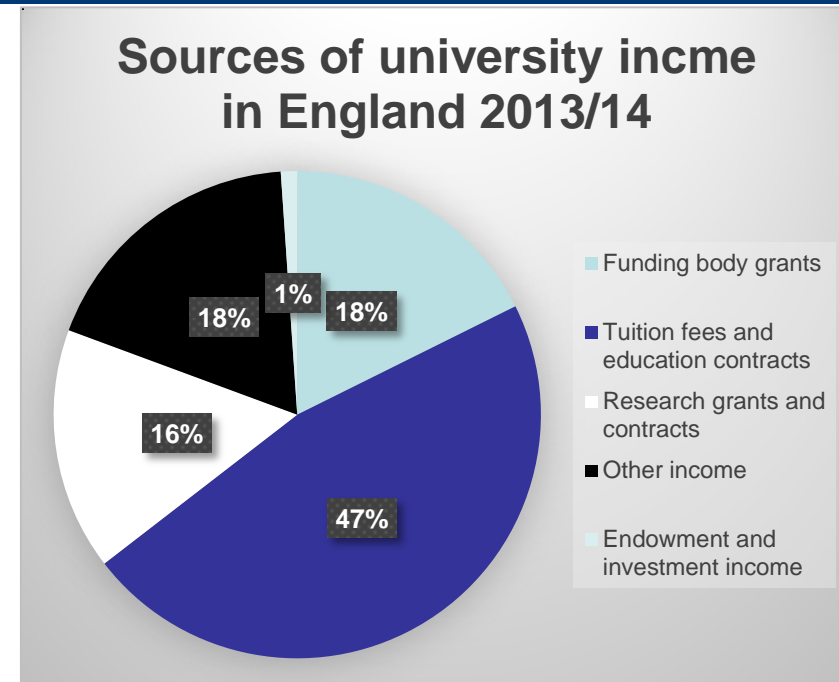
# Outline of talk

- 1. Introduction**
- 2. Literature review**
- 3. Conceptual issues**
- 4. Model specification**
  - Defining the variables
  - Estimation method
- 5. Results**
  - Estimated average costs
  - Economies of scale
  - Economies of scope
  - Efficiencies
- 6. Conclusions**

[https://www.gov.uk/government/uploads/system/uploads/attachment\\_data/file/237411/bis-13-918-efficiency-in-higher-education-sector.pdf](https://www.gov.uk/government/uploads/system/uploads/attachment_data/file/237411/bis-13-918-efficiency-in-higher-education-sector.pdf)

# 1. Introduction

- HEIs receive public money
  - funding body grants
  - non-payment of tuition fees
- Reduced incentive to be efficient
- Need to assess efficiency of higher education institutions (HEIs)
- Cost functions provide information on efficiency, economies of scale and economies of scope



# 1. Introduction

The English higher education sector comprises very diverse groups of HEIs:

- ✓ Pre-1992 universities: degree programmes in all academic subjects; research mission
- ✓ Post-1992 universities: degree programmes in academic and vocational subjects; many have a research mission
- ✓ Former colleges of HE: small, specialist HEIs; most do not have a research mission

# 1. Introduction

## Questions

- What are average and marginal costs of outputs of English HEIs?
- Are there economies of scale and scope in English HE?
- How efficient are English HEIs?
- How does 'mission group' affect costs?
- Are there other factors which might affect HEIs' costs?

## 2. Literature Review

- USA: Cohn *et al* (1989)
- UK: Glass *et al* (1995a; 1995b); Johnes (1996; 1997; 1998); Izadi *et al* (2002); Stevens (2005); Johnes *et al* (2005; 2008); Thanassoulis *et al* (2011)
  - ✓ Relatively low efficiency in panel data studies
  - ✓ Efficiency varies by type of university
  - ✓ Ray economies of scale; diseconomies of scope
  - ✓ Student quality, location of HEI are not important determinants of costs

## 2. Literature Review

### Most recent developments (RPM and LCM)

- USA: Agasisti & Johnes (2009) use latent class model (LCM) with SFA
  - ✓ Allows objectives *to vary by group* suggested by the data
- UK: Johnes & Johnes (2009) use a random parameter model (RPM) with SFA
  - ✓ Allows *each HEI* to have different objectives
- Findings:
  - ✓ HEIs are heterogeneous in terms of both cost structure and efficiency



# 3. Conceptual Issues

## Functional form of cost function

a) Linear:  $C = \alpha_0 + \sum_i \beta_i y_i$

b) Quadratic:  $C = \alpha_0 + \sum_i \alpha_i F_i + \sum_i \beta_i y_i + \left(\frac{1}{2}\right) \sum_i \sum_j \gamma_{ij} y_i y_j + v$

# 3. Conceptual Issues

Denote by  $C(y)$  the total cost of producing all  $N$  outputs

$C_i(y)$  the marginal cost of output  $i$

$AIC(y_i)$  the average incremental cost of output  $i$

where  $AIC(y_i) = [C(y) - C(y_{N-i})]/y_i$

**Ray economies of scale**  $S_R = \frac{C(y)}{\sum_i y_i C_i(y)}$

✓ If  $S_R > 1$  ( $< 1$ ) then there are economies (diseconomies) of scale

# 3. Conceptual Issues

**Product-specific economies of scale**  $S_i(y) = AIC(y_i)/C_i(y)$

- ✓ If  $S_i > 1$  ( $< 1$ ) then there are economies (diseconomies) of scale for product  $i$

**Economies of scope**  $S_G = [\sum_i C(y_i) - C(y)]/C(y)$

- ✓ If  $S_G > 0$  ( $< 0$ ) then global economies (diseconomies) of scope exist for producing the outputs jointly rather than in separate institutions

# 4. Model Specification

## a) Outputs

### TEACHING

- **UGMED** FTE undergraduates in medicine and dentistry (000s)
- **UGSCI** FTE undergraduates in sciences other than medicine and dentistry (000s)
- **UGARTS** FTE undergraduates in non-science subjects (000s)
- **PG** FTE postgraduates in all subjects (000s)

# 4. Model Specification

## a) Outputs

### RESEARCH

- **RESEARCH** Quality related funding and research grants

### THIRD MISSION

- **IPINCOME** Income from third mission activity

**Note that** all squares and interactions of UGMED, UGSCI, UGARTS, PG and RESEARCH are included; the square of IPINCOME and interaction of IPINCOME only with RESEARCH are included.

# 4. Model Specification

## b) Additional factors

### QUALITY OF STUDENTS

- **MEANSAL** Mean salary of graduates 6 months after graduation

### QUALITY OF TEACHING

- **NSS** Percentage saying yes to the question: 'Overall, I am satisfied with the quality of the course' from the National Student Survey

### WIDENING PARTICIPATION

- **LOWPNO** Number of FT UG entrants from 'low participation' neighbourhoods

# 4. Model Specification

## b) Additional factors

### ESTATES COSTS

- **LISTED** The total area of the HEI identified as a listed building

### DUMMY VARIABLES

- **OXBRIDGE** Dummy variable: 1 if HEI is Oxford or Cambridge
- **YEAR** Dummy for each year in the study (apart from the last)

# 4. Model Specification

- SFA

For HEI  $i$  at time  $t$ :

$$C_{it} = f(y_{1it}, \dots, y_{kit}) + v_{it} + u_{it}$$

- SFA with latent class model (LCM)

For HEI  $i$  at time  $t$ ,  $m$  classes:

$$C_{it} = f_m(y_{1it}, \dots, y_{kit}) + v_{it,m} + u_{it,m}$$



# 5. Results

- Panel data from 2008/09 to 2010/11 covering around 120 HEIs
- Efficiency is allowed to vary over time within any given model
- Data are largely from the Higher Education Statistics Agency
- All money units are in 2011 values

# 5. Results

## AIC from SFA linear model (2011 £)

AICs	2008/09 to 2010/11		
		Class 1	Class 2
<b>UGMED</b>	13484	10865	7774
<b>UGSCI</b>	7775	1931	8472
<b>UGARTS</b>	4574	9353	2757
<b>PG</b>	13953	246	18694
<b>No. in each class</b>		121	234

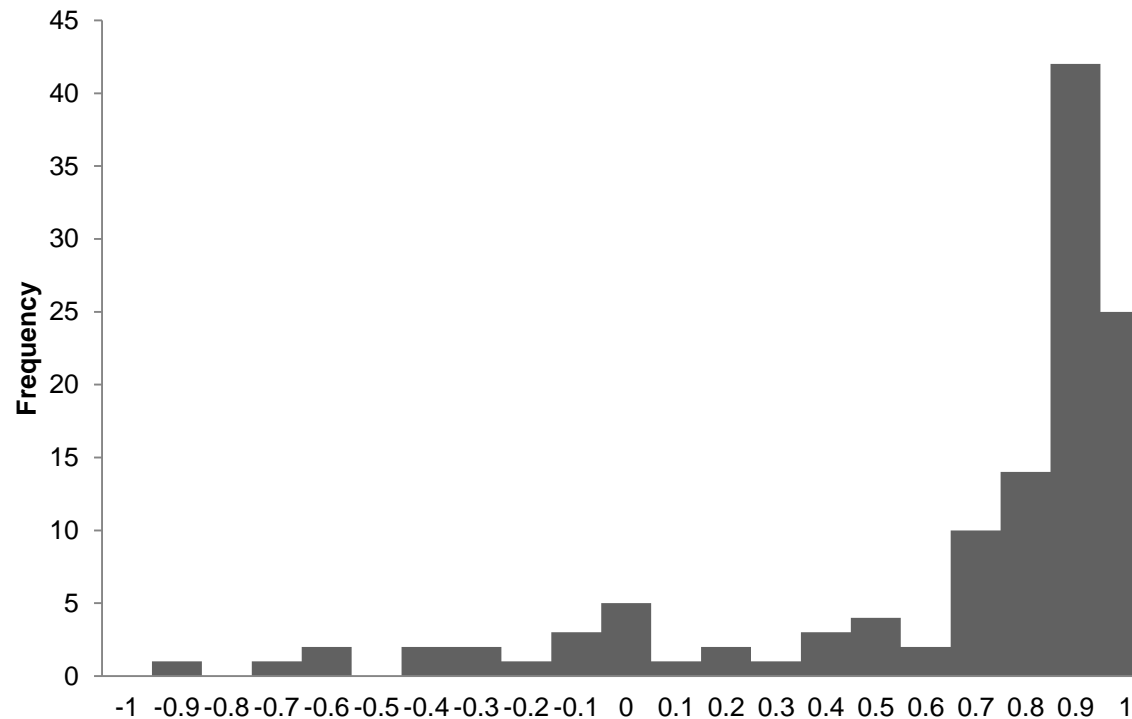
Other outputs included: RESEARCH, IPINCOME

Controls for: LISTED, LOWPNO, YEAR dummies,  
OXBRIDGE

# 5. Results

## Histogram of efficiency scores

### 2010/11 linear model

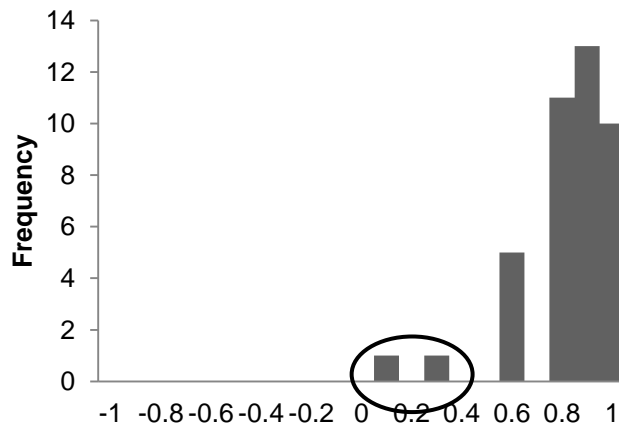


# 5. Results

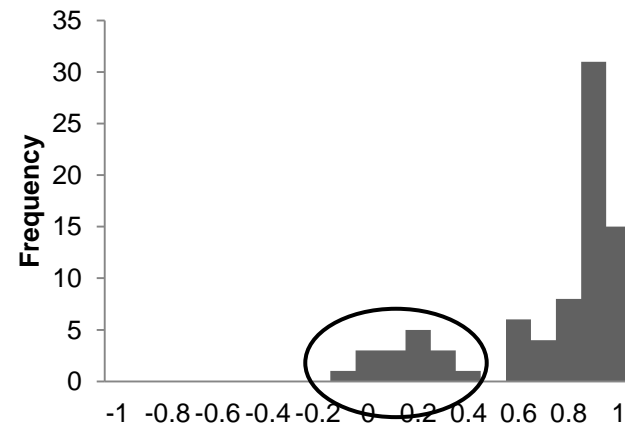
## Histogram of efficiency scores

### 2010/11 linear model

#### Latent class 1



#### Latent class 2



# 5. Results

## Akaike Information Criterion (AkIC)

$$AkIC = -2.\log LF(m) + 2.k$$

where k is the number of estimated parameters

No. of classes	2008/09 to 2010/11
1	8393.3
2	7711.9
3	7637.9
4	7561.9

## 5. Results

### AIC from SFA quadratic model (2011 £)

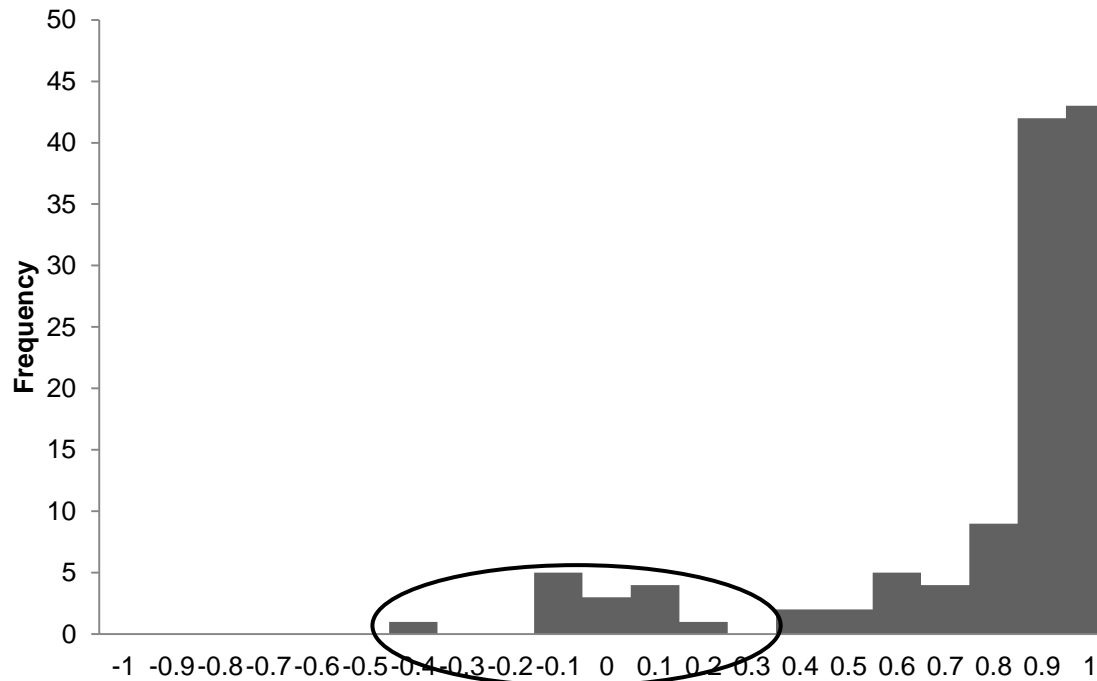
AICs	2008/09 to 2010/11		
		Class 1	Class 2
<b>UGMED</b>	16034	8720	19595
<b>UGSCI</b>	7858	5260	7185
<b>UGARTS</b>	5459	5883	2176
<b>PG</b>	5275	7839	1242
<b>No in each class</b>		236	119

Other outputs included: RESEARCH, IPINCOME  
 Controls for: LISTED, LOWPNO, YEAR dummies,  
 OXBRIDGE

# 5. Results

## Histogram of efficiency scores

### 2010/11 quadratic model

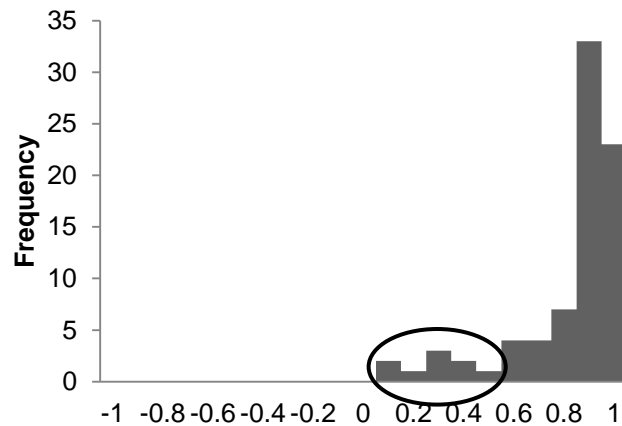


# 5. Results

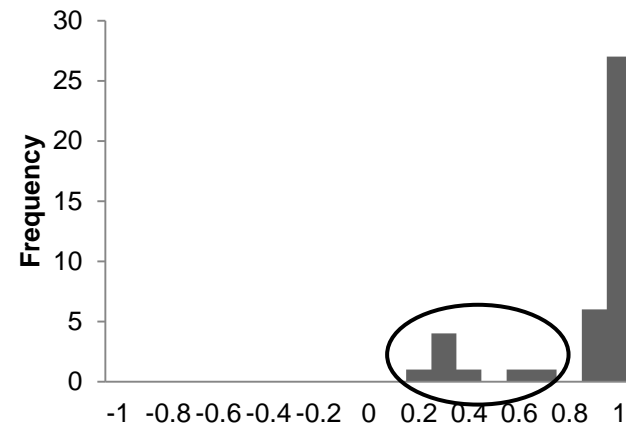
## Histogram of efficiency scores

### 2010/11 quadratic latent class model

#### Latent class 1



#### Latent class 2





# 5. Results

## Comparison of Models with Akaike Information Criterion (AkIC)

$$\text{AkIC} = -2.\log\text{LF}(m) + 2.k$$

where k is the number of estimated parameters

No. of classes	2008/09 to 2010/11
1	-661.0
2	-848.9
3	-915.9

# 5. Results

## Economies of scale and scope

### Quadratic model: HEI with mean levels of output)

	SFA	SFA class 1	SFA class2
<b>Scale</b>			
Ray economies	1.01	0.95	0.97
UGMED	1.25	1.11	1.23
UGSCI	1.00	1.26	0.75
UGARTS	1.23	0.84	0.46
PG	0.78	0.60	0.25
RESEARCH	1.13	0.97	1.00
IPINCOME	1.09	1.12	1.00

# 5. Results

## Economies of scale and scope

### Quadratic model: HEI with mean levels of output)

	SFA	SFA class 1	SFA class2
<b>Scale</b>			
Ray economies	1.01	0.95	0.97
UGMED	1.25	1.11	1.23
UGSCI	1.00	1.26	0.75
UGARTS	1.23	0.84	0.46
PG	0.78	0.60	0.25
RESEARCH	1.13	0.97	1.00
IPINCOME	1.09	1.12	1.00
<b>Scope</b>			
Global economies	-0.01	-0.13	-0.01

## 6. Conclusions

- Estimates of AICs from SFA models seem plausible
- Estimates of AICs from SFA LCM seem less precise
- Ray economies of scale are exhausted; there are product specific economies in UG teaching and in research
- There are diseconomies of scope
- Efficiency differences are much lower once other (observed and unobserved) characteristics are taken into account
- A low efficiency score is usually explained by HEI being small and/or specialist
- What allowances should be made in determining efficiency?