Current limiting and negative differential resistance in indium oxide based ceramics

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Abstract.

Indium oxide based ceramics with bismuth oxide addition were sintered in air in the temperature range 800-1300 °C. Current-voltage characteristics of In₂O₃-Bi₂O₃ ceramics sintered at different temperatures are weakly nonlinear. After an additional heat treatment in air at about 200 °C samples sintered at a temperature within the narrow range of about 1050-1100 °C exhibit a current-limiting effect accompanied by low-frequency current oscillations. It is shown that the observed electrical properties are controlled by the grain-boundary barriers and the heat treatment in air at 200 °C leads to the decrease in the barrier height. Electrical measurements, scanning electron microscopy and X-ray photoelectron spectroscopy results suggest that the current-limiting effect observed in In₂O₃-Bi₂O₃ may be explained in terms of a modified barrier model; the observed current-limiting effect is the result of an increase of barrier height with increasing electric field, due to additional oxygen absorption. It is found that In₂O₃-Bi₂O₃-Cr₂O₃-Cr₂O₃ ceramic exhibits current-voltage characteristics with negative differential resistance due to Joule micro heating.

Keywords: A. Sintering; B. Grain Boundaries; C. Electrical Properties; Indium Oxide; E. Varistors.

1 Introduction

At low electric fields the current-voltage characteristic of a sample is generally linear and Ohm’s law is obeyed. An increase in the electric field can cause some deviations from Ohm’s law. Two cases are possible: superlinear, exploited in varistors, where the current rises more strongly than voltage, or sublinear where current rises more weakly than voltage. The nonlinear current-voltage characteristic can be approximated by the empirical equation

\[ I = BU^\beta, \]  

where \( I \) is the current, \( U \) is the voltage, \( \beta \) is the nonlinearity coefficient \( \beta = (U/I)(dI/dU) \) and \( B \) is some constant. In the case of superlinear current-voltage characteristic \( \beta > 1 \) and in the case of sublinear current-voltage characteristic \( \beta < 1 \).

At the present time, sublinear current-voltage characteristics have been found in some polycrystalline materials [1-7] and several explanations of this effect were suggested [1,3,8-11]. In particular, such behaviour has been observed in In₂O₃-SrO ceramics [5,6]. In this material the addition of strontium leads to an increase in resistivity at low electric fields and the appearance of non-Ohmic behaviour (saturation and even decrease in current density) at higher fields. The mechanism of this current limiting effect in In₂O₃-SrO ceramics can be related to the increase in the grain-boundary barrier height with applied electric field due to the additional oxygen adsorption [12].

However, in In₂O₃-SrO ceramics quite strong degradation is observed and, as a result, the current limiting effect disappears after some time. From a materials science view-point it would be interesting to study indium oxide based non-Ohmic ceramics with other additives, with the aim to produce a more
Indium oxide exhibits n-type conduction and is widely used for the preparation of transparent electrodes for optoelectronic devices [13-15] and gas-sensors [16-18]. However, it is well known that the addition of bismuth oxide (Bi₂O₃) improves the sintering and promotes an increase in the nonlinearity coefficient in zinc oxide based and tin dioxide based varistor ceramics [19-24]. This suggests that bismuth oxide addition may also induce non-ohmic behavior in indium oxide ceramics. Moreover, some bismuth oxide phases in such ceramics can have ionic conduction with oxygen ion as a carrier [25-27] this can be favourable for the manifestation of the current limiting mechanism proposed by Bondarchuk et al. [12].

To investigate this idea, we present a study of the electrical properties and microstructure of indium oxide based In₂O₃-Bi₂O₃ ceramics sintered at different temperatures and with different post-production heat-treatment processes.

2 Experimental Method

Indium oxide based ceramics (mol.%) 95In₂O₃-5Bi₂O₃ were prepared by the conventional mixed oxides method [5,24] with sintering at temperature in the wide range of 800-1300 °C. Ceramics (mol.%) 98.5In₂O₃-0.5Bi₂O₃-0.5CoO₂-0.5Cr₂O₃ were sintered at 1200 °C.

A Zeiss Supra 35VP field emission scanning electron microscope (FE-SEM) was used to obtain secondary electron, backscattered electron (BSE) and in-lens images of sample surfaces, fracture surfaces and polished cross-sections. Elemental composition information from BSE data were augmented with energy dispersive X-ray microanalysis (EDX) obtained with Oxford Instruments INCA system attached to the SEM. Accelerating voltages of 5keV were utilized to enable elemental analysis whilst ensuring low penetration depth. X-ray photoelectron spectroscopy (XPS) was performed with a VG EscaLab210 (Al anode), the composition of the surface was calculated from high resolution expansions utilising empirically derived atomic sensitivity factors [28]. X-ray diffraction was conducted with a Bruker D8 AXS spectrometer.

The density, ρ, of sintered samples was determined using hydrostatic weighting method in distilled water. The theoretical density \( \rho_T = 7.294 \text{ g cm}^{-3} \) of the studied material was calculated taking into account the chemical composition before sintering. It was assumed that physical and chemical processes during sintering have negligible effect on the chemical composition. The closed porosity was estimated from the expression

\[
\rho_C = 1 - \rho \cdot \rho_T^{-1}.
\]

Ag-electrodes fired in air at 800 °C were used [24]. An additional heat treatment was conducted in air at 800 °C for 1 hour with slow heating and slow cooling. An additional heat treatment in air atmosphere at 200 °C was performed by slowly heating a sample with Ag-electrodes up to 200 °C, maintaining this temperature for 1 hour and subsequently quenching to room temperature.

Current-voltage characteristics were studied, utilizing a Keithley-237 unit. At automatic recording voltage was applied during 10 ms (current was measured at the end of this interval) and the voltage was reduced to zero for a period of 100 ms. Electric field \( E_{-5} \) was calculated at the current density \( j = 1 \cdot 10^{-5} \text{ A cm}^{-2} \).

Current-voltage characteristics of the samples with negative differential resistance were studied in the “current source” regime. In this case rectangular current pulses with successively increasing and decreasing amplitude (current increment \( 1 \cdot 10^{-5} \text{A} \)) were used. Two examination modes were employed. In mode A, sample overheating was avoided by using a short pulse duration 10 ms with a pause between pulses 1 s. In mode B, sample overheating was achieved using pulse duration 4 s with a pause between pulses 4 s.
Small-signal capacitance versus dc voltage was measured using a QuadTech 7600 LCR meter and a Keithley 6487 voltage source, both controlled by computer. Rectangular voltage pulses with increasing amplitude (voltage increment 5 V, pulse duration 4 s, pause between pulses 4 s) were used. Capacitance was measured at frequency 100 Hz with ac voltage amplitude 0.5 V. The run “down” gives the same data.

Temperature dependence of dc electrical conductivity \( \sigma(T) \) was obtained in the range of 290-370 K in air by heating and cooling of a sample with a rate of about 1.5 K/min. The activation energy of electrical conduction \( E_\sigma \) was found from the equation:

\[
\sigma(T) = \sigma_0 \exp\left(\frac{-E_\sigma}{kT}\right)
\]

where \( \sigma \) is the electrical conductivity, \( \sigma_0 \) is a constant, \( k \) is the Boltzmann´s constant, \( T \) is the absolute temperature.

### 3 Experimental Results and Discussion

#### 3.1 Sintering Temperature

SEM micrographs of samples obtained at different sintering temperature are shown in figure 1. The grain size increases with sintering temperature; for example, in the sample sintered at 1100 °C (figure 1 b) grains in the range 0.5-2 \( \mu \)m are observed, in contrast to the sample sintered at 800°C (figure 1 a) where the grain size is 200 - 500 nm. Analysis of both as-sintered surfaces (figures 1 a, c) and fracture cross sections (for example, figure 1 b) shows grains in sample bulk are similar in size and morphology to those at the sinter surface. Analysis of lower magnification SEM images (such as figure 1 d) shows the porous nature of the samples. The density of sintered samples are:

- \( \rho = 4.972 \text{ g} \cdot \text{cm}^{-3} \) (sintering temperature 800°C),
- \( \rho = 5.206 \text{ g} \cdot \text{cm}^{-3} \) (1100°C) and
- \( \rho = 5.896 \text{ g} \cdot \text{cm}^{-3} \) (1300°C). The closed porosity was estimated from these results as 31.8% (800°C), 28.6% (1100°C) and 19.2% (1300°C).

SEM backscattered electron analysis of a polished section of the sample sintered at 1100°C, in conjunction with the topography information from the in-lens image of the same area, shows a distinct, atomically heavier phase at a proportion of the grain boundaries. Analysis of elemental composition by EDX shows indium oxide grains with predominantly bismuth oxide at the grain boundaries. XRD measurements are consistent with bismuth oxide as a boundary phase, rather than incorporated into \( \text{In}_2\text{O}_3 \) lattice. This is consistent with \( \text{Bi}_2\text{O}_3 \) addition responsible for liquid-phase sintering.

Current-voltage characteristics of \( \text{In}_2\text{O}_3\)-\( \text{Bi}_2\text{O}_3 \) ceramics sintered at different temperatures (fig.2) are weakly superlinear (\( \beta > 1 \)). The increase in sintering temperature causes a decrease in the low-field conductivity (at 800-1050°C) followed by an increase at 1050-1300°C. This means that electric field, \( E_{\text{s,s}} \), at fixed current density (\( j = 1 \cdot 10^{-5} \text{ A cm}^{-2} \)) passes through a maximum (fig.3, curve 1).

If conduction is controlled by the grain-boundary barriers, then the barrier height in this case should also pass through a maximum. If we additionally assume that the Fermi level in the bulk of indium oxide grains is situated not more than several tenths of eV below the conduction band edge and, therefore, the barrier height \( \varphi \) in the studied \( \text{In}_2\text{O}_3\)-\( \text{Bi}_2\text{O}_3 \) ceramics is only slightly less than the activation energy \( E_\sigma \) of electrical conduction, \( \varphi \approx E_\sigma \), then one can expect that the activation energy also should pass through the maximum. Experimental data confirm such assumption: the activation energy for different sintering temperatures indeed goes through a maximum at 1100°C (fig.3, curve 2).

Probably, due to n-type conduction in indium oxide, the increase in sintering temperature up to 1100°C leads to some growth in oxygen content at the grain boundaries related to the presence of liquid \( \text{Bi}_2\text{O}_3 \) though at higher temperatures the evaporation of bismuth oxide becomes significant and oxygen content at the grain boundaries is decreased. In any case, the observed correlation supports the assumed barrier
conduction mechanism: the higher the barrier height, the lower the conductivity (Fig.2) and, therefore, the higher the electric field at fixed current density (Fig.3, curve 1).

3.2 Additional Heat Treatments. In the samples sintered at different temperatures, sublinear I(U) and current oscillations were not initially manifested. It has been shown previously [29] that in In$_2$O$_3$-Bi$_2$O$_3$ ceramics obtained at 1100 °C, current limiting and low-frequency current oscillations effects appeared after a heat treatment in air at about 200 °C with sharp cooling. Therefore, samples sintered at different temperatures were subjected to the additional heat treatment at 200 °C. It was observed that samples sintered at 1050 and 1100°C exhibit sublinear current-voltage characteristics, relatively weak in the sample sintered at 1050°C and quite strong for the sample sintered at 1100°C (Fig.4). Samples sintered at other temperatures retain the slight superlinearity of current-voltage characteristic, even after the additional heat treatment. Low-frequency current oscillations accompany the observed sublinearity but to avoid some complexity, current-voltage characteristics in the sublinear region are presented using average current values. The current limiting effect and low-frequency current oscillations are reproducible.

The reproducibility in current-voltage characteristics of the sample sintered at 1100 C and additionally heat treated at 200 C to generate the current limiting effect is illustrated in Fig.5. Voltage increase (Fig.5, curve 1) and decrease (Fig.5, curve 2) give nearly the same I(U) characteristics. This current-voltage characteristic is symmetric (Fig. 5, curves 1 and 3). At voltages higher than about 50 V the scattering of experimental points is observed. It is due to the current oscillations. In In$_2$O$_3$-Bi$_2$O$_3$ ceramics the current limiting effect is always accompanied by low-frequency current oscillations and both phenomena are quite reproducible. The degradation of the current-voltage characteristics after numerous measurements in In$_2$O$_3$-Bi$_2$O$_3$ ceramics is significantly less than was found in In$_2$O$_3$-SrO ceramics [12]. Therefore, In$_2$O$_3$-Bi$_2$O$_3$ ceramics have substantial advantages in comparison to In$_2$O$_3$-SrO ceramics as a material where the current limiting effect is observed.

So far we relate both the current limiting effect and current oscillation to the grain-boundary barriers, which appear in these ceramics as a result of sintering in the oxidizing atmosphere. The additional heat treatment at 200 °C affects electrical properties of the samples sintered at 1100°C; it would therefore be interesting to study the effect of this heat treatment on the barrier height. As shown in figure 6, the heat treatment in air at 200C with rapid quenching causes the barrier height to decrease for all sintering temperatures. An additional heat treatment in air at 800 °C causes barrier height to increase, equally or exceeding initial values. The barrier height as a function of sintering temperature has a maximum at about 1050-1100°C regardless of the subsequent heat-treatment process.

The system with decreased barrier height after the heat treatment in air at 200°C appears to be quite stable. Similar time-stability of electrical properties was observed in SnO$_2$-ZnO-Bi$_2$O$_3$ varistor ceramics after the heat treatment in air at 200-400 °C [21]. Only an increase in applied electric field causes additional oxygen absorption resulting in an increase of barrier height as electric field increases, thus causing the observed current-limiting effect.

The observed decrease in the barrier height after the heat treatment in air at 200°C could be explained by a decrease in oxygen content at the grain boundaries. Therefore, to further explore the oxygen content in the sample we studied XPS spectra of the samples sintered at 1100 °C, with and without additional heat treatment in air at 200°C. There is a slight increase in the relative oxygen content of the sample surface following heat-treatment; however, this can most likely be related to the decrease in hydrocarbon contamination on the sample surface, as there is no significant change in the ratio of oxygen content to the sum of the indium and bismuth contents. More noticeably, the XPS data show a change in the indium:bismuth ratio at the sample surface; this ratio increases by a factor of approximately 1.4 following heat treatment at 200°C. There is no concurrent shift in the photoelectron peak position, indicating at most only a negligible change in the oxidation state. This alteration in the surface chemistry is not accompanied by a change in the morphology, or by a change in the bulk In:Bi ratio as detected by EDX – a technique with a penetration depth in the order of micrometres, rather than the 1 - 10nm analysis depth of XPS. However, the EDX spectra do suggest some change in the oxygen content within the grains, suggesting the heat treatment and rapid quench do cause some redistribution of the oxygen within the ceramic. Although the difference in oxygen content is not entirely clear, we believe that the change in chemistry of the grain boundaries with additional heat treatment processes results in the observed current-limiting...
effect, the result of an increase in barrier height with applied electric field, caused by additional oxygen absorption [12].

The current limiting effect observed in the In$_2$O$_3$-Bi$_2$O$_3$ ceramics studied here is markedly different from the electrical properties of ZnO-Bi$_2$O$_3$-based [20,22] or SnO$_2$-Bi$_2$O$_3$-based ceramics [21,23,24], which exhibit the varistor effect. In both groups of materials the grain-boundary barriers play the main role in the conduction process. The varistor effect in ZnO-based and SnO$_2$-based materials is related to the lowering of the barrier height with increase in electric field [30-34]. But perhaps the feature of barriers to be decreased (in varistor ceramics) or increased (in ceramics with current limiting behaviour) with the application of voltage depends on the specific impurities at the grain boundaries. Thus, an alteration of the grain-boundary impurities could change the electrical properties of such ceramics.

To examine this, In$_2$O$_3$-Bi$_2$O$_3$-Co$_2$O$_4$-Cr$_2$O$_3$ ceramics were sintered. Cobalt and chromium oxides additives were chosen to reproduce the favorable conditions for obtaining of varistor ceramics in a system ZnO-Bi$_2$O$_3$-Sb$_2$O$_3$-Co$_2$O$_4$-MnO-Cr$_2$O$_3$ with a high nonlinearity coefficient $\beta \approx 50$ [20]. Current-voltage characteristics of the obtained sample are shown in Fig.7. In contrast to In$_2$O$_3$-Bi$_2$O$_3$ samples, current-voltage characteristics are superlinear and can be varistor-type (Fig.7, curves 1-2) or can be superlinear and contain a region with negative differential resistance $R_d = dU/dI < 0$ (in the case if measurements are performed permitting overheating of a sample) (Fig.7, curves 3-4). Earlier current-voltage characteristics with switching or negative differential resistance were observed in various non-oxide and oxide systems (see, for example [34,35]).

In spite of the strong difference between two types of superlinear curves each current-voltage characteristic is quite reproducible for increase and decrease of voltage (Fig.7, curves 1-2 and curves 3-4). Though, in the case of negative differential resistance (Fig.7, curves 3-4) some hysteresis is found due to thermic mechanism of the negative differential resistance effect. The sensitivity of current-voltage characteristic to the variation of voltage pulse duration, a wide current region with negative differential resistance and the absence of a region with positive differential resistance at higher current (Fig.7) confirm the thermic nature of observed negative differential resistance effect.

For additional confirmation of the thermic nature of this negative differential resistance effect, low-frequency capacitance versus dc voltage was obtained (Fig.7, curve 5). In the case of negative differential resistance related to Joule heating the low-frequency capacitance should becomes negative (inductive behaviour of ac current) [36]. Indeed, negative capacitance is detected, even at low voltages when overheating only begins.

4 Conclusions

In$_2$O$_3$-Bi$_2$O$_3$ ceramics with current-limiting effect (sublinear I(U) dependence, nonlinearity coefficient $< 1$) are investigated. The materials were sintered in air in the temperature range 800-1300 °C. The grain size increases with increase in sintering temperature. It is found that sublinear I(U) characteristics are observed only in In$_2$O$_3$-Bi$_2$O$_3$ ceramics sintered at a temperature within the narrow range of about 1050-1100 °C, and with subsequent heat treatment in air at 200 °C with rapid quenching. It is shown that the observed electrical properties are controlled by the grain-boundary barriers and the heat treatment leads to the decrease in the barrier height. Electrical measurements, scanning electron microscopy and X-ray photoelectron spectroscopy results suggest that the current-limiting effect observed in In$_2$O$_3$-Bi$_2$O$_3$ can be explained in terms of the modified barrier model proposed earlier for the explanation of similar effect in In$_2$O$_3$-SrO ceramics. It is found that In$_2$O$_3$-Bi$_2$O$_3$-Co$_2$O$_4$-Cr$_2$O$_3$ ceramic material exhibits current-voltage characteristics with negative differential resistance due to Joule micro heating.
Acknowledgements

This study was performed in part in the frames of the project SEP-2003-C02-42821, CONACYT, México. Funding from the Royal Society, United Kingdom (2007R1/R26999) is gratefully acknowledged. We thank L. Anguilano for technical assistance.

References

Fig.1. SEM micrographs of In$_2$O$_3$-Bi$_2$O$_3$ ceramics sintered at (a) 800°C, (b) 1100°C and (c) 1300°C. SEM images of as-sintered surfaces (a, c) and fracture surfaces (b, d) show grain size distribution and porosity.

Fig.2. Current-voltage characteristics of In$_2$O$_3$-Bi$_2$O$_3$ ceramics sintered at different temperatures.
Fig. 3. (1) electric field at fixed current density and (2) activation energy of conduction versus sintering temperature

Fig. 4. Effect of the heat treatment in air at 200°C on current-voltage characteristics of In$_2$O$_3$-Bi$_2$O$_3$ ceramics sintered at different temperatures

Fig. 5. Current-voltage characteristics of the sample In$_2$O$_3$-Bi$_2$O$_3$ sintered at 1100 C and additionally heat treated at 200 C. I(U) characteristics are obtained at increase (1) and decrease (2) of voltage and at opposite polarity (3). Current limiting is accompanied by current oscillations.
Fig. 6. Activation energy of electrical conduction versus $T_{\text{SINT}}$ measured after the additional heat treatment in air (1) at 800 °C (during formation of electrodes) then (2) at 200 °C and then (3) at 800 °C again.

Fig. 7. Current (1-4) and capacitance (5) versus dc voltage for $\text{In}_2\text{O}_3$-$\text{Bi}_2\text{O}_3$-$\text{Co}_3\text{O}_4$-$\text{Cr}_2\text{O}_3$ ceramics. An overheating of a sample is absent (1 - at voltage increase, 2 - at voltage decrease). An overheating of a sample takes place (3 - at voltage increase, 4 - at voltage decrease).