NOx Prediction Based on Cylinder Pressure Measurement for Engine Emission Monitoring

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ABSTRACT

Meeting European NOx emission standards is one of the biggest challenges facing automotive industries. The available technologies to measure NOx emission are dependent on measurement of different NOx species. In addition, in most cases it requires conversion of other NOx species to NO for measurement purposes. The ability to measure NOx emission on-line during the transient engine operation may be very difficult due to the delay in reaction time in the NOx measuring apparatus. NO\(_x\) emissions in compression ignition (CI) engines are largely a thermal phenomena thus cylinder pressure is key to making accurate predictions of NOx. If cylinder pressure data is available the heat release during combustion can be modeled and thus NO\(_x\) emission can be more accurately simulated. Therefore, the main objective of this study is to investigate the performance of the cylinder pressure in predicting the NOx emission from a CI engine running with biodiesel during both steady and transient operations. To address the problem experimental work has been conducted on a four-cylinder, four-stroke, direct injection (DI) and turbocharged diesel engine. In this investigation, biodiesel (produced from the rapeseed oil by transesterification process) has been used. During the experiment the in-cylinder pressure, TDC mark, fuel flow rate, air flow rate and the NOx emission were measured. The temperature within the cylinder was predicted using the cylinder pressure. Using the temperature values the NOx emission was simulated in Zeldovich extended mechanism. The measured and simulation results of NOx emission were compared during steady state conditions and shows maximum error of 4.5%.

Keywords: NOx emission, In-Cylinder Pressure, In-Cylinder Temperature, Biodiesel

1. INTRODUCTION

Oxides of Nitrogen are one of the most undesirable pollutant constituents of automotive transport because of its connection with the formation of photochemical smog in the atmosphere. It is also the major toxic emission that are being regulated with both in EU and USA emission regulations becoming more and more stringent (Aithal 2010); Dieselnet 2010; (C. Lin & H. Lin 2006).

NOx formation pathway includes three methods, i.e., thermal NOx, fuel NOx, and prompt NOx. Even though the degree of the emission release amount varies, each of the three pathways of NOx formation contributes to the overall NOx emission to the environment (Fuent, Inc 2003; Fernando et al. 2006). The thermal NOx, is the main contributor to NOx emissions from a diesel engine. It is formed during fuel combustion in the combustion cylinders when the atmospheric oxygen and nitrogen combine at a high temperature (Kornbluth et al. 2009; Trogler et al. 1997; K & M 2009). The general equation for the formation of NOx can be described by equations (1-3) as described as the Zeldovich extended mechanism (Newhall 1969). To analysis the phenomena of NOx generation in diesel engine, detailed knowledge of
the temperature and reaction mechanisms for fuel pyrolysis, NOx, and unburnt carbon-hydrogen formation in the engine cylinder during the compression and power strokes (Mellor et al. 1998; Aithal 2010) are required.

\[ \text{N}_2 + O \xrightarrow{K_1} NO + N \] (1)

\[ N + O_2 \xrightarrow{K_2} NO + O \] (2)

\[ N + OH \xrightarrow{K_3} NO + H \] (3)

The currently available methods of measuring/predicting NOx emissions include analyzer (direct measuring), engine map method, and artificial neutral network. Measurement of Oxides of nitrogen on a dry basis, by means of a heated chemiluminescent detector (HCLD) with a NO2/NO analyzer is widely used. However, the analyzer has disadvantages of higher associated costs, requiring large space, demanding frequent calibration and possible effects of soot. In addition, its responses are very slow, which affect the transient NOx emission measurement (Krijnsen et al. 1999). However, the formation of NO is the most significant phenomena under transient engine operations. This effects are mainly seen during engine acceleration or load acceptance, owing to the momentary increase in fuel injection which contributes to higher cycle temperatures and, hence NO production (Armas et al. 2006; Samuel et al. 2007). An engine map is a NOx database generally based on measurements of a series of settings of engine speed and torque or power of the engine under stationery conditions. Most of the maps have the disadvantages that the map does not consider all the significant variables on the NOx emission levels. This may cause deviations between the real NOx emissions estimated from the engine map. In addition, it will estimate the transient conditions from the discrete steady state values (Krijnsen et al. 1999). The third method which needs the artificial neural network (ANN) system has advantage of avoiding in using the NOx emission models, and work with transient conditions. However, in the neural network there is no explicit mathematical representation of the physical process and the predicting capability is limited only to specific engine type for which the neural network trained (S H Chan 1999).

The in-cylinder pressure measurement is considered a very valuable source of information during the development, testing and condition monitoring stages of engine development (Payri et al. 2010). NOx emission in CI engines is largely a thermal phenomenon and thus cylinder pressure can be used to make an accurate prediction of NOx quantity in real time, which will utilize of in-cylinder measurement. Therefore the main objective of this study is to investigate a novel approach to using the cylinder pressure for predicting the NOx emission of a CI engine running with biodiesel during both steady and transient operations.

2. MODEL FORMULATION

The main task of this study is to use the in-cylinder pressure measurement to predict the NOx emission from the CI engine. Generally, it has been well established the dominate process that produces NO in CI engine combustion. It is the thermal mechanism, which occurs in the post-flame burned gases, and described by the extended Zeldovich mechanism which described by equations (1-3) including the reactants, products and rate constants. In order to drive the rate of change of NO concentration, it was assumed that the concentration of the N is minor in comparison with the concentrations of the other species, so that the rate of change in N can be set equal to zero. Using this assumption and after some mathematical rearranging the rate of NO concentration, denoted as [NO], is given by equation (4).

\[
\frac{d[NO]}{dt} = 2k_1[O][N_2] \left( \frac{k_{-1}k_{-2}[NO]^2}{k_1[N_2]k_2[O_2]} + \frac{k_{-1}[NO]}{k_2[O_2]+k_3[OH]} \right) \text{ g mol/(m}^3\text{s)}
\] (4)

The rate constants for these reactions have been measured in numerous studies and critically evaluated (Mellor et al. 1998; Aithal 2010; Fuent, Inc 2003), and the reaction rates used in this NOx model
are given in Table (1). In Table 1 the (-) sign indicate the backward reaction. The \([N_2]\) and \([O_2]\) concentrations were determined at ambient condition of the atmospheric air.

Table 1 Rate constants for thermal NOx formation (Fuent, Inc 2003)

<table>
<thead>
<tr>
<th>Rate constants</th>
<th>Values ([\text{m}^3/(\text{gmol s})])</th>
</tr>
</thead>
<tbody>
<tr>
<td>(k_1)</td>
<td>(1.8 \times 10^8 e^{-\frac{38370}{T}})</td>
</tr>
<tr>
<td>(k_{-1})</td>
<td>(3.8 \times 10^7 e^{-\frac{425}{T}})</td>
</tr>
<tr>
<td>(k_2)</td>
<td>(1.8 \times 10^4 T e^{-\frac{4680}{T}})</td>
</tr>
<tr>
<td>(k_{-2})</td>
<td>(3.8 \times 10^3 T e^{-\frac{20820}{T}})</td>
</tr>
<tr>
<td>(k_3)</td>
<td>(7.1 \times 10^8 e^{-\frac{450}{T}})</td>
</tr>
<tr>
<td>(k_{-3})</td>
<td>(1.7 \times 10^9 e^{-\frac{24560}{T}})</td>
</tr>
</tbody>
</table>

The concentration of oxygen \([O]\) by equation (5) and (6) and the maximum value was taken. Similarly, the \([OH]\) was estimated by equation (7).

\[
[O] = 3.97 \times 10^5 T^{-1/2} [O_2]^{1/2} e^{-31090/T} \quad \text{g mol/m}^3 \quad (5)
\]

\[
[O] = 36.64 T^{1/2} [O_2]^{1/2} e^{-27123/T} \quad \text{g mol/m}^3 \quad (6)
\]

\[
[OH] = 2.129 \times 10^2 T^{-0.57} [O_2]^{1/2} [H_2]^{1/2} [O]^{1/2} e^{-45957/T} \quad \text{g mol/m}^3 \quad (7)
\]

To predict the thermal NOx emission from the in-cylinder temperature the ideal-gas equation of state which described in equation (8) was used.

\[
T(\theta) = \frac{P(\theta) V(\theta)}{M(\theta) R_g}
\]

(8)

Where, \(T(\theta)\) is the instantaneous in-cylinder temperature(K), \(P(\theta)\) is the instantaneous in-cylinder pressure(Pa), \(M(\theta)\) is the instantaneous mass in cylinder (kg), \(R_g\) is gas constant (J/kg·K) and \(V(\theta)\) is the instantaneous cylinder volume (m³) calculated by equation (9).

\[
V(\theta) = \frac{V_d}{r_c} + \frac{V_d}{2} \left[ R + 1 - \cos \theta - (R^2 - \sin^2 \theta)^{1/2} \right]
\]

(9)

Where \(V_d\) is displacement volume given \(R\) is the ratio of connecting rod length to crank radius and \(r_c\) is compression ratio.

The model was simulated numerically using a Matlab program under different engine operation conditions explained in section 3.
3. EXPERIMENTAL FACILITIES AND TEST PROCEDURE

In this study the in-cylinder pressure, fuel mass flow rate, air flow rate and NOx emission were measured and used in the NOx prediction model and for validation purposes. The engine used in the present investigation is a four-cylinder, four-stroke, turbo-charged, water-cooled and direct-injection CI engine. Full details of parameters of the engine are included in table 2. The load to the engine was provided by a 200kW AC Dynamometer with 4-Quadrant regenerative drive with motoring and absorbing capability for both steady and transient conditions. It is integrated with speed sensors, pressure transducers, thermocouples, air flow meters, fuel flow meters and in-line torque meter. A Hengler RS58 speed sensor was used to measure the speed of the engine. The air-consumption was measured using hot-film air-mass meter HFMS and the fuel consumption was measured by FMS-1000 gravimetric fuel measuring which was controlled and monitored by CADETV12 software. The cylinder pressure was measured using Kistler 6125A11 model air-cooled piezo-quartz pressure sensor which was mounted on the cylinder head. The cylinder pressure signal was passed through Bruel & Kjaer 2635 charge amplifier. The crankshaft position was obtained using a crank angle sensor to determine the cylinder pressure as a function of the crank angle.

All the signals collected from the test rig needed to be converted from an original analogue form to a digital form. This was achieved by using a Cambridge Electric Design (CED) Power 1401 Analogue to Digital Converter (ADC) interface between the transducers and the computer. The Analogue to Digital Converter (ADC) has 16 channels and 500 MHz bandwidth. The fuel from biodiesel tank was pumped to a fuel meter and, then it was passed through a fuel pump to the fuel injectors. The scheme of the test rig layout with the basic instrumentations is shown in figure 1.

The measurement of the gaseous emissions was carried out using a gas test bench HORIBA, Horriba EXSA - 1500. It has measuring range of 0 – 5000ppm and an error of 1%. The sample line of the equipment is connected directly to the exhaust pipe and it is heated to maintain a wall temperature of around 191°C and avoid condensation of hydrocarbons. The insulated line is extended from the exhaust pipe to the

![Figure 1 Experimental setup](image-url)
equipment unit where the analyzers are located. Oxides of nitrogen are measured on a dry basis, by means of a heated chemiluminescent detector (HCLD) with a NO\textsubscript{2}/NO converter.

During the testing process the engine was initially run for 10 minutes to bring it to a steady state before any measurements were carried out. On the day prior to the actual test day and also in between test regimes with different fuel type, a preconditioning procedure was implement that included running the engine at a high load and then at a low load to purge out any of the remaining effects from previous tests in the engine fuel system and also to remove the deposited hydrocarbon from the sample line. The frequency of the data acquisition system was 37kHz. The sampling time used was 40 seconds. The operating conditions used in the tests are listed on Table 3. The operating conditions were selected with an aim to cover main engine operating speeds and loads as per the New European Driving Cycle (NEDC).

Table 2 Characteristics of engine

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td>Engine type</td>
<td>Turbo charged diesel engine</td>
</tr>
<tr>
<td>Number of cylinders</td>
<td>4</td>
</tr>
<tr>
<td>Bore</td>
<td>103mm</td>
</tr>
<tr>
<td>Stroke</td>
<td>132mm</td>
</tr>
<tr>
<td>Compression ratio</td>
<td>18.3</td>
</tr>
<tr>
<td>Number of valves</td>
<td>16</td>
</tr>
<tr>
<td>Injection system</td>
<td>Direct injection</td>
</tr>
<tr>
<td>Displacement</td>
<td>4.399 liter</td>
</tr>
<tr>
<td>Cooling system</td>
<td>Water</td>
</tr>
</tbody>
</table>

Table 3 Operating conditions

<table>
<thead>
<tr>
<th>Condition</th>
<th>Speed(rpm)</th>
<th>Load(Nm)</th>
<th>Fuel</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>900</td>
<td>105, 210, 315, 420</td>
<td>Diesel, Biodiesel</td>
</tr>
<tr>
<td>B</td>
<td>1100</td>
<td>105, 210, 315, 420</td>
<td>Diesel, Biodiesel</td>
</tr>
<tr>
<td>C</td>
<td>1300</td>
<td>105, 210, 315, 420</td>
<td>Diesel, Biodiesel</td>
</tr>
<tr>
<td>D</td>
<td>1500</td>
<td>105, 210, 315, 420</td>
<td>Diesel, Biodiesel</td>
</tr>
</tbody>
</table>

The biodiesel used in this study was rapeseed oil biodiesel purchased from a local biodiesel producer. The biodiesel was produced by transesterification process from ‘virgin’ oil using methanol. The main physical properties such as composition, density, lower heating value and viscosity of the biodiesel were measured in the applied science laboratory according to the official test standards and are shown in Table 4.
4. RESULT AND DISCUSSION

To predict the NOx emission from the measured in-cylinder pressure using ideal-gas state equation, the in-cylinder pressure and the in-cylinder temperature characteristics of the combustion are described. The comparison of the in-cylinder pressure and in-cylinder temperature of diesel and biodiesel fuel are also discussed in detail. Finally the predicted NOx emissions values from in-cylinder pressure measurement were compared with measured NOx emission for both diesel and biodiesel fuel.

Figure 2(a) shows that the in-cylinder pressure within the combustion chamber of the CI engine running with 100B (100% Bio-diesel) at a speed of 1300 rpm and engine loads of 105Nm, 210Nm, 315Nm and 420Nm. The results show that the peak cylinder pressure of the engine increases with increasing the load from 105Nm to 420Nm.

![Figure 2(a) 1300rpm](image)

(a) 1300rpm

![Figure 2(b) 420Nm](image)

(b) 420Nm

Figure 2 In-cylinder pressure at different crank angle (a) at 1300 rpm and various load( b) at 420Nm and various engine speed.

Table 4 Physical and Chemical properties of fuel

<table>
<thead>
<tr>
<th>Property</th>
<th>Units</th>
<th>Diesel</th>
<th>Biodiesel</th>
</tr>
</thead>
<tbody>
<tr>
<td>% C</td>
<td></td>
<td>87</td>
<td>77</td>
</tr>
<tr>
<td>Composition</td>
<td>% H</td>
<td>13</td>
<td>12</td>
</tr>
<tr>
<td></td>
<td>% O</td>
<td>0</td>
<td>11</td>
</tr>
<tr>
<td>Density</td>
<td>Kg m$^{-3}$</td>
<td>853</td>
<td>879</td>
</tr>
<tr>
<td>Lower heating value(LHV)</td>
<td>MJ Kg$^{-1}$</td>
<td>42679</td>
<td>38500</td>
</tr>
<tr>
<td>Viscosity, mm$^2$/s</td>
<td>mm$^2$s$^{-1}$</td>
<td>3.55</td>
<td>5.13</td>
</tr>
</tbody>
</table>
The cylinder produces the minimum peak in-cylinder pressure of 6.5MPa at 105Nm and the maximum in-cylinder pressure of 8.8 MPa at 420Nm. The effects of the engine speed on the in-cylinder pressure within the combustion chamber of the CI engine running with 100B at a load of 420Nm and various engine speeds are depicted in figure 2(b). The results show that the peak of cylinder pressure of the engine increases with increasing the engine speed.

The biodiesel combustion flame temperature values, which have been calculated from the instantaneous in-cylinder pressure, cylinder volume and air flow rate, are depicted in figure 3(a) and figure 3(b) for different engine speeds and loads ranges respectively. It can be seen, in figure 3(a), that when the load increases the in-cylinder temperature also increases. Similarly, when the engine speed increases the in-cylinder pressure also increases. It can be concluded from the above that when the engine speed and load increase the in-cylinder pressure increases. Even though, the cylinder volume and cylinder pressure are inversely proportionally, since the change magnitude of the in-cylinder pressure is higher, its effect dominate the in-cylinder temperature values. In Figure 3(b) it can be seen that generally the in-cylinder temperature increases with increasing the speed up to engine speed of 1300rpm.

Figure 3 In-cylinder temperature at different crank angle (a) at 1300 rpm and various load (b) at 420Nm and various engine speed.

Figure 4 shows that the in-cylinder pressure within the combustion chamber of the CI engine running with diesel and 100B at different engine speeds and engine load of 420Nm. The results show that the peak cylinder pressure of the engine running with biodiesel is slightly higher than the engine running with diesel. The main cause for higher peak in-cylinder pressure in the CI engine running with biodiesel is because of the advanced combustion process initiated by easy flow-ability of bio-diesel due to the physical properties of the biodiesel. In addition, due to the presence of oxygen molecule in the biodiesel, the hydrocarbons achieve complete combustion (Canakci 2007; Gumus 2010) resulting in higher in-cylinder pressure.

Figure 5 shows the in-cylinder temperature for biodiesel and diesel operating conditions. The result shows that the flame temperature corresponding to biodiesel operation is higher than the diesel operation. The higher temperature of the biodiesel is caused due to the availability of additional oxygen molecule as mentioned earlier. As it will be discussed later this is the main cause for the higher emission.
of NOx. On the contrary, Monyem et al (Monyem et al. 2001) reported that for both constant-volume combustion and constant-pressure combustion, the flame temperature for biodiesel is slightly below that for diesel fuel.

Figure 4 In-cylinder pressure of the CI engine running by biodiesel and diesel at 420Nm and different engine speed

![Graph showing in-cylinder pressure for different engine speeds.](image)

Figure 5 In-cylinder temperature of the CI engine running by biodiesel and diesel at 420Nm and different engine speed

![Graph showing in-cylinder temperature for different engine speeds.](image)

The predicted NOx emission corresponding to the biodiesel operation at a load of 315Nm and various engine speeds are shown in figure 6. The NOx emissions were found to decrease with the increase in the
engine speed. This can be explained as at higher engine speed, the volumetric efficiency and gas flow motion within the engine cylinder are increased. These lead to faster mixing between air and fuel and minimize the ignition delay (C. Lin & Chen). As a result the nitrogen and oxygen molecule resident time is reduced.

![Figure 6 Predicted NOx emission at 315Nm and various engine speeds](image)

Figure 6 Predicted NOx emission at 315Nm and various engine speeds

Figure 7 shows the predicted value of nitrogen oxides (NOx) emission for engine running with biodiesel and diesel at 315Nm load for speed of 900rpm, 1100rpm, 1300rpm and 1500rpm. It can be seen that the NOx emission when running with biodiesel is higher than that of the diesel by 5, 10, 17 and 7% respectively. The main reason for higher emission of biodiesel is the advanced combustion process initiated because of the physical properties of biodiesel (viscosity, density, compressibility, sound velocity) (Lapuerta et al. 2008; Wang et al. 2000). When biodiesel is injected, the pressure rise produced by the pump is quicker as a consequence of its lower compressibility (higher bulk moduls) and propagate more quickly towards the injectors. As a result, the cylinder gas becomes rich fairly quickly by fuel and reaches its peak temperature which speeds up the formation NOx.

To investigate the accuracy of the NOx prediction model from the cylinder pressure, the measured and the predicted value of NOx are presented in table 1. It can be seen from the table that maximum deviation of the model from the measured one is 4.06% for diesel and 4.39% for biodiesel.
Table 5 Measured and Predicted NOx emission values at 315Nm

<table>
<thead>
<tr>
<th>Speed(rpm)</th>
<th>Diesel(ppm)</th>
<th>Biodiesel(ppm)</th>
<th>Diesel Deviation</th>
<th>Biodiesel Deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Measured</td>
<td>Predicted</td>
<td>Measured</td>
<td>Predicted</td>
</tr>
<tr>
<td>900</td>
<td>1020</td>
<td>1002</td>
<td>1050</td>
<td>1094</td>
</tr>
<tr>
<td>1100</td>
<td>850</td>
<td>850</td>
<td>910</td>
<td>896</td>
</tr>
<tr>
<td>1300</td>
<td>715</td>
<td>686</td>
<td>730</td>
<td>719</td>
</tr>
<tr>
<td>1500</td>
<td>615</td>
<td>637</td>
<td>670</td>
<td>660</td>
</tr>
</tbody>
</table>

CONCLUSION

In this study, the performance of using the cylinder pressure to predict the NOx emission has been investigated based on a compression ignition (CI) engine running with different fuels including biodiesel. The temperature of the cylinder is predicted firstly using the cylinder pressure by ideal-gas state equation. Using the predicted temperature the NOx emission is then calculated based the Zeldovich extended mechanism. The measured and prediction results of NOx emission are compared and it has been shown that the deviation of the values obtained from the model from the measured values is less than to 4.06% for diesel and 4.39% for biodiesel respectively. Moreover, the reasons for higher NOx emission
from biodiesel have been explored based on the predication. The prediction paves the way of real-time NOx emission estimation for engine transient study and online diagnosis.

Reference


